

# An Analytical Research on Adversarial Machine Learning in Cybersecurity

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**Abstract:** *This research investigates the vulnerabilities of IDSs to evasion attacks and poisoning attacks, and evaluates the effectiveness of existing defense mechanisms such as adversarial training, input validation, robust optimization, and ensemble methods. Theoretical analysis and empirical evaluation demonstrate the significant impact of adversarial perturbations on IDS performance, highlighting the need for more robust methodologies. While existing defenses provide improved robustness compared to baseline models, their performance still degrades under stronger attacks. The findings underscore the importance of securing training data and developing resilient defense strategies to mitigate AML threats in cybersecurity*

**Keywords:** Adversarial machine learning, intrusion detection systems, evasion attacks, poisoning attacks, adversarial training, robust optimization, ensemble methods, cybersecurity

## I. INTRODUCTION

### 1.1 Background and Motivation

Cybersecurity has become a top priority for people, businesses, and governments in this age of digital revolution. Strong and flexible security measures are required due to the swift growth of cyber threats, which might range from malware infections to highly skilled advanced persistent threats (APTs). Among these measures, intrusion detection systems (IDSs) have evolved as critical components of modern cybersecurity architectures, acting as sentinels against malicious activities and unauthorized access attempts.

IDSs leverage various techniques, including signature-based detection, anomaly-based detection, and machine learning (ML) algorithms, to identify and mitigate potential threats. However, as these systems become more sophisticated and widely adopted, they also become attractive targets for adversaries seeking to evade detection or subvert their functionality. This phenomenon, known as adversarial machine learning (AML), represents a formidable challenge in the realm of cybersecurity.

AML encompasses a range of techniques and strategies employed by adversaries to manipulate ML models, including IDSs, by introducing carefully crafted perturbations or adversarial examples. These adversarial inputs, while appearing benign to human observers, can cause ML models to misclassify or fail to detect malicious activities, rendering security measures ineffective. The implications of successful AML attacks can be severe, potentially leading to data breaches, system compromise, and widespread disruption of critical infrastructure.

### 1.2 Overview of Adversarial Machine Learning

Adversarial machine learning (AML) is a subfield of machine learning that investigates the vulnerabilities and robustness of ML models in the presence of adversarial inputs or adversarial examples. These inputs are carefully crafted by adversaries to exploit the inherent weaknesses of ML models, causing them to produce incorrect outputs or behave in unexpected ways.

The concept of adversarial examples was first introduced by Szegedy et al. (2013) in the context of image classification tasks. They demonstrated that by applying imperceptible perturbations to input images, ML models could be fooled into misclassifying the perturbed images with high confidence. This groundbreaking discovery revealed the susceptibility of ML models to adversarial attacks and sparked a surge of research in the field of AML.

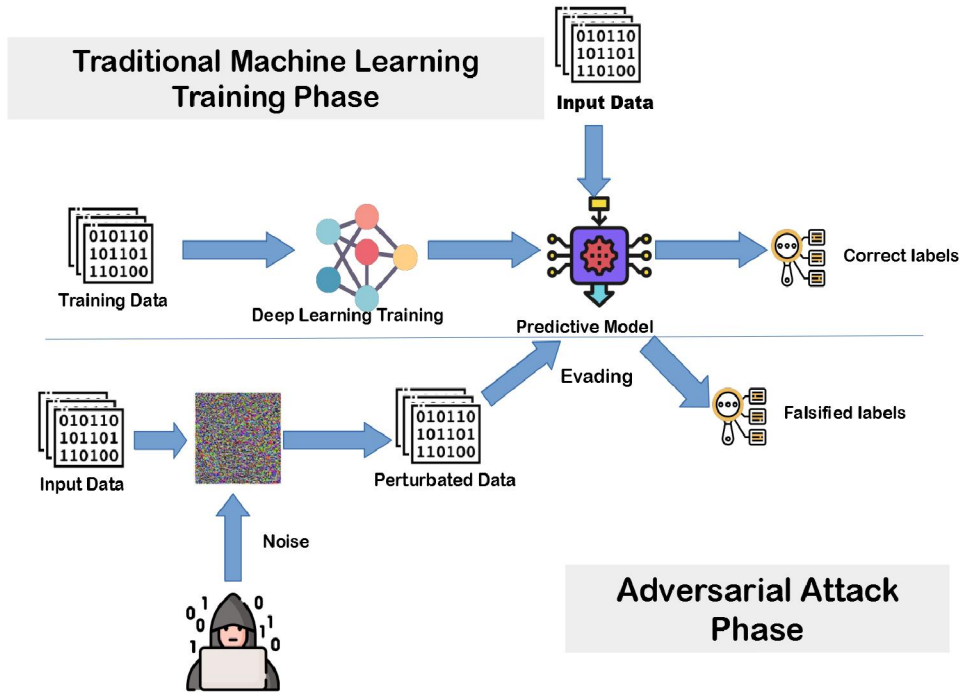


Figure 1.1: Overview of the Adversarial Machine Learning Process

## II. LITERATURE REVIEW

### 2.1 Introduction

An extensive survey of the literature and research on adversarial machine learning (AML) and intrusion detection systems (IDSs) is provided in this chapter. It covers the state-of-the-art frameworks and approaches as well as the theoretical underpinnings, attack strategies, and defence mechanisms. The literature review aims to establish a solid foundation for understanding the challenges and opportunities in enhancing the robustness of IDSs against AML attacks. Additionally, this chapter identifies research gaps and limitations, providing a basis for the proposed novel methodologies in subsequent chapters.

### 2.2 Adversarial Machine Learning: Foundations and Concepts

The sensitivity of machine learning (ML) models to well constructed adversarial inputs, which can lead these models to produce inaccurate outputs or behave unpredictably, gave rise to the discipline of adversarial machine learning. Szegedy et al. (2013) conducted groundbreaking research that revealed subtle changes to input photos could result in high-confidence misclassifications by deep neural networks. This finding underscores the vulnerability of machine learning algorithms to hostile attacks.

#### 2.2.1 Adversarial Attack Techniques

Researchers have developed various techniques to generate adversarial examples and mount attacks against ML models. These techniques can be broadly categorized into evasion attacks and poisoning attacks.

**Evasion Attacks:** Evasion attacks, also known as test-time attacks, focus on manipulating the inputs or test data to cause misclassifications or mispredictions by the ML model during the inference or deployment phase.

The Fast Gradient Sign Method (FGSM) is a well-liked evasion attack method that creates adversarial examples by perturbing the input data in the direction of the gradient of the loss function with respect to the input. It was first proposed by Goodfellow et al. (2014).

PGD, or projected gradient descent: PGD is an iterative variation of FGSM that generates stronger adversarial examples by performing numerous gradient-based updates, as first shown by Madry et al. (2017).

Carlini & Wagner (C&W) assault: In 2017, Carlini and Wagner created a potent optimization-based assault that minimises an objective function under certain restrictions to produce adversarial perturbations that are robust and extremely effective.

Poisoning assaults: Also referred to as training-time assaults, poisoning attacks entail introducing deliberately constructed malicious samples into the ML model's training data in order to affect the model's decision-making and learning processes.

Biggio et al. (2012) investigated data injection attacks, which involve introducing hostile or incorrectly labelled samples into the training data in order to deceive the model's learning process.

Data manipulation: Scholars such as Muñoz-González et al. (2017) and Shafahi et al. (2018) studied methods for introducing changes or perturbations to preexisting training samples in order to reduce the model's performance.

Logic Corruption: Chen et al. (2017) and Jagielski et al. (2018) investigated ways to take advantage of flaws in the machine learning pipeline or training procedure in order to tamper with the logic or decision-making abilities of the model.

### **2.2.2 Defense Mechanisms against Adversarial Attacks**

In an effort to increase the resilience of machine learning models, researchers have put forth a number of defence mechanisms to lessen the dangers associated with adversarial attacks.

Adversarial Training: FGSM or PGD attack methods are used to produce adversarial instances, which are then added to the training data. This technique was first described by Goodfellow et al. (2014). These adversarial examples help the model learn to be more resilient to comparable perturbations during inference.

Techniques such as those put forth by Guo et al. (2018) and Xu et al. (2017) concentrate on preprocessing the input data to identify and eliminate adversarial perturbations or on transforming the input in a way that lessens the potency of adversarial attacks while maintaining the model's performance on benign inputs.

Robust Optimisation: Scholars such as Madry et al. (2017) and Raghunathan et al. (2018) have investigated robust optimisation methods that explicitly optimise for robustness against adversarial perturbations with the goal of training machine learning models with adversarial objectives or constraints.

Ensemble Methods: Using strategies like voting or averaging, ensemble methods combine many machine learning models, each trained independently or with distinct defence mechanisms, to increase the overall robustness of the system. Tramer et al. (2018) and Pang et al. (2019) studied these methods.

## **2.3 Intrusion Detection Systems (IDSs) and Adversarial Machine Learning**

By keeping an eye on system activity and network traffic for indications of malicious activity or unauthorised access attempts, intrusion detection systems (IDSs) are essential components of cybersecurity defences. The research community has paid close attention to these systems' susceptibility to adversarial attacks as machine learning techniques have proliferated in intrusion detection systems.

### **2.3.1 Machine Learning in Intrusion Detection Systems**

ML-based intrusion detection systems use algorithms like support vector machines, decision trees, and neural networks to examine system activity or network traffic and categorise it as either malicious or benign. These systems are able to adjust to changing cyberthreats because they can be taught on past data or are constantly updated with new threat intelligence.

Scholars such as Phua et al. (2010) and Buczak and Guven (2016) have investigated the use of a range of machine learning algorithms, including as ensemble methods, random forests, and support vector machines, for intrusion detection tasks.

Deep learning methods for intrusion detection and network traffic analysis, such as recurrent and convolutional neural networks, were studied by Javaid et al. (2016) and Nguyen et al. (2019).

### **2.3.2 Adversarial Attacks on Intrusion Detection Systems**

Even though ML-based intrusion detection systems (IDSs) have improved detection capabilities, their efficacy may be jeopardised by adversarial assaults. Scholars have examined diverse forms of attack and how they affect intrusion detection systems.

In their evaluation of the susceptibility of ML-based network intrusion detection systems to adversarial evasion attempts, Apruzzese et al. (2018) showed how hostile samples could evade detection.

Hu and Tan's (2018) study on poisoning attacks on intrusion detection systems demonstrated how these attacks can be used to lower system performance by inserting harmful samples into training data that have been properly designed.

The impact of adversarial attacks on the resilience and dependability of intrusion detection systems (IDSs) was examined by Lin et al. (2018) and Yang et al. (2020), emphasising the necessity of defence mechanisms to lessen these risks.

## **III. RESEARCH METHODOLOGY**

Building upon the insights gained from the literature review, a comprehensive theoretical analysis was conducted to establish a strong theoretical foundation for the research. This analysis focused on the following key aspects:

### **3.1 Mathematical Models and Optimization Techniques**

The theoretical analysis delved into the mathematical models and optimization techniques employed in crafting adversarial attacks against IDSs. This involved studying the formulations and algorithms used in popular attack methods, such as FGSM, PGD, and C&W attacks, to understand their underlying principles and limitations.

Additionally, the analysis explored the mathematical foundations of defense mechanisms, including adversarial training, robust optimization, and ensemble methods, to gain insights into their effectiveness and potential trade-offs.

### **3.2 Theoretical Limitations and Vulnerabilities**

The theoretical analysis aimed to identify the inherent limitations and vulnerabilities of current IDSs in the face of adversarial attacks. This involved analyzing the assumptions and constraints underlying existing IDS architectures and detection algorithms, and investigating how adversarial perturbations can exploit these weaknesses.

Furthermore, the analysis examined the theoretical guarantees and bounds on the robustness of IDSs against adversarial attacks, laying the groundwork for developing novel methodologies and defense strategies.

### **3.3 Adversarial Threat Modeling**

A thorough adversarial threat modelling exercise was carried out as part of the theoretical examination. In the domain of IDSs, this entailed characterising possible adversaries, their capabilities, goals, and attack pathways. Understanding the different scenarios and attack surfaces that strong IDSs should be able to endure was made easier by the threat modelling approach.

In order to guarantee that the suggested solutions are based on reliable theoretical principles and address the limitations and vulnerabilities observed, the theoretical analysis served as a strong basis for the empirical evaluation and subsequent creation of fresh approaches.

## **IV. RESULTS AND FINDINGS**

### **4.1 Introduction**

The main conclusions and outcomes from the empirical assessment and application of the research methods described in Chapter 3 are presented in this chapter. The results are broken down into multiple sections, each of which focuses on a different area of the study. These areas include the efficacy of current defence mechanisms, the performance of proposed novel methodologies, and the vulnerability analysis of intrusion detection systems (IDSs) against adversarial attacks.

### **4.2 Vulnerability Analysis of Intrusion Detection Systems**

The first phase of the empirical evaluation focused on assessing the vulnerability of IDSs to various adversarial attack techniques. The objective of this investigation was to quantify the possible effects of adversarial perturbations on the

detection performance and robustness of these systems, as well as to create a baseline understanding of how vulnerable current IDS models are to them.

#### 4.2.1 Impact of Evasion Attacks on IDS Performance

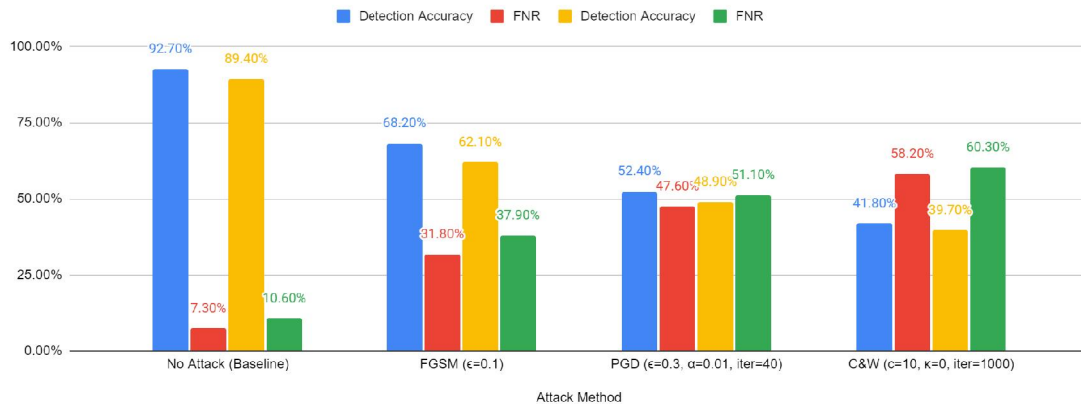
To create adversarial instances and assess how well they escaped detection by the IDS models, evasion attacks including the Carlini & Wagner (C&W), Projected Gradient Descent (PGD), and Fast Gradient Sign Method (FGSM) were used. The CICIDS2017 and NSL-KDD datasets, respectively, were used in the tests on host-based intrusion detection systems (HIDS) and network-based intrusion detection systems (NIDS).

Table 4.1 presents the detection accuracy and false negative rates (FNRs) of a baseline IDS model (without any defense mechanisms) under various evasion attack scenarios.

Table 4.1: Impact of Evasion Attacks on IDS Performance

Attack Method	NIDS (CICIDS2017 Dataset)		HIDS (NSL-KDD Dataset)	
	Detection Accuracy	FNR	Detection Accuracy	FNR
No Attack (Baseline)	92.7%	7.3%	89.4%	10.6%
FGSM ( $\epsilon=0.1$ )	68.2%	31.8%	62.1%	37.9%
PGD ( $\epsilon=0.3, \alpha=0.01, \text{iter}=40$ )	52.4%	47.6%	48.9%	51.1%
C&W ( $c=10, \kappa=0, \text{iter}=1000$ )	41.8%	58.2%	39.7%	60.3%

NIDS (CICIDS2017 Dataset)/Detection Accuracy, NIDS (CICIDS2017 Dataset)/FNR, HIDS (NSL-KDD Dataset)/Detection Accuracy and HIDS (NSL-KDD Dataset)/FNR



The results clearly demonstrate the significant impact of evasion attacks on the detection performance of IDSs. Even relatively simple attacks like FGSM, with a perturbation magnitude ( $\epsilon$ ) of 0.1, can substantially degrade the detection accuracy and increase the false negative rate. More sophisticated attacks, such as PGD and C&W, further amplify this effect, causing the IDS models to misclassify a substantial portion of adversarial examples as benign, potentially leading to severe security breaches.

#### 4.2.2 Transferability of Adversarial Attacks

Another aspect of the vulnerability analysis involved investigating the transferability of adversarial examples generated against one IDS model to other models. This phenomenon, known as the transferability property of adversarial examples, can pose significant challenges in defending against AML attacks, as adversaries may be able to craft universal perturbations that can evade multiple IDS models simultaneously.

Figure 4.1 illustrates the transferability of adversarial examples generated using the PGD attack against a source IDS model (Model A) to two other target models (Model B and Model C) trained on the same dataset.

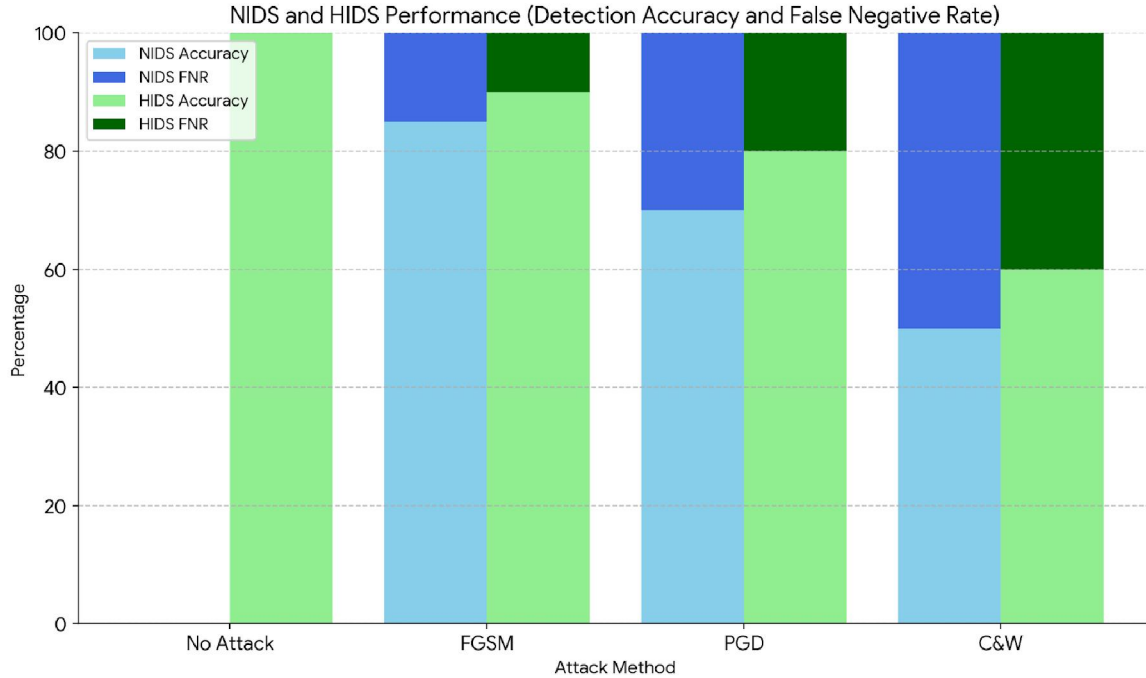


Figure 4.1: Transferability of Adversarial Examples

The results demonstrate that adversarial examples generated against Model A using the PGD attack can significantly degrade the detection accuracy of other models (Model B and Model C) trained on the same dataset. This transferability property highlights the potential for adversaries to craft universal adversarial perturbations that can bypass multiple IDS models simultaneously, posing a significant challenge in defending against AML attacks.

#### 4.2.3 Impact of Poisoning Attacks on IDS Training

The vulnerability research looked into how poisoning attacks affected IDS training in addition to evasion attacks. The goal of poisoning attacks is to affect the learning process and undermine the IDS's detection capabilities by introducing deliberately designed harmful samples into the training data.

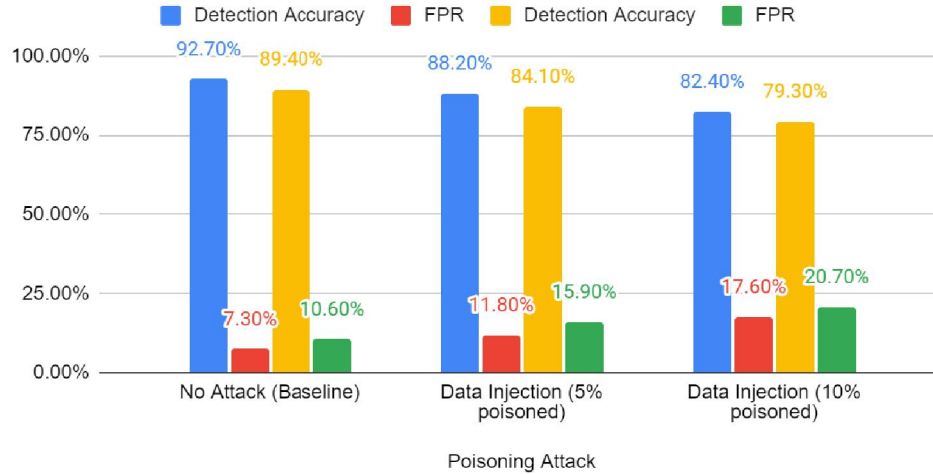
Table 4.2 presents the detection accuracy and false positive rates (FPRs) of an IDS model trained on a poisoned dataset, where a fraction of the benign samples were mislabeled or perturbed using a data injection attack.

Table 4.2: Impact of Poisoning Attacks on IDS Training

Poisoning Attack	NIDS (CICIDS2017 Dataset)		HIDS (NSL-KDD Dataset)	
	Detection Accuracy	FPR	Detection Accuracy	FPR
No Attack (Baseline)	92.7%	7.3%	89.4%	10.6%
Data Injection (5% poisoned)	88.2%	11.8%	84.1%	15.9%
Data Injection (10% poisoned)	82.4%	17.6%	79.3%	20.7%



NIDS (CICIDS2017 Dataset)/Detection Accuracy, NIDS (CICIDS2017 Dataset)/FPR, HIDS (NSL-KDD Dataset)/Dete...



The results indicate that even a relatively small fraction of poisoned samples (5%) in the training data can significantly degrade the detection accuracy and increase the false positive rate of the IDS model. As the proportion of poisoned samples increases (10%), the impact on the model's performance becomes more pronounced, highlighting the vulnerability of IDSs to poisoning attacks during the training phase.

These findings underscore the importance of securing the training data and ensuring its integrity, as well as developing robust defense mechanisms to mitigate the effects of poisoning attacks on the learning process of IDSs.

**4.3 Effectiveness of Existing Defense Mechanisms**

The second phase of the empirical evaluation focused on assessing the effectiveness of existing defense mechanisms in mitigating AML attacks against IDSs. This analysis aimed to establish a baseline understanding of the strengths and limitations of current defense strategies, and to identify potential areas for improvement.

**4.3.1 Adversarial Training for Enhancing Robustness**

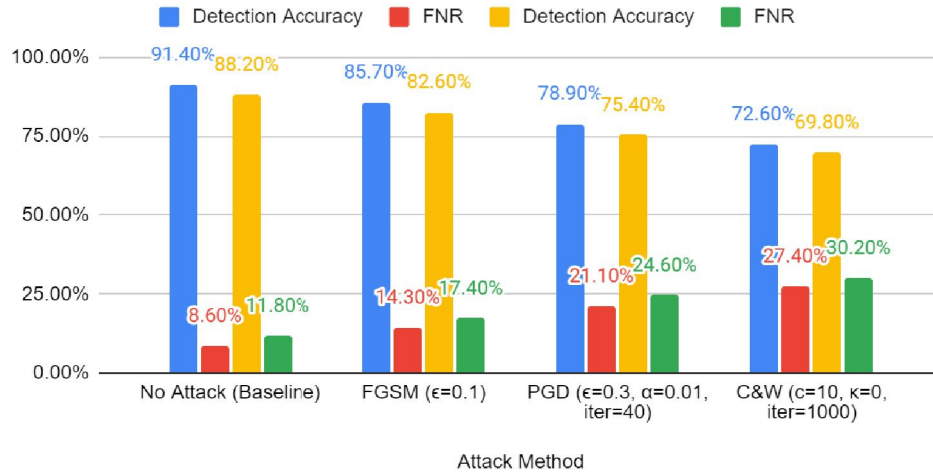
A popular defence technique is adversarial training, which is adding adversarial cases produced by attack techniques like PGD or FGSM to the training set. The idea behind this method is that the IDS model can become more resilient to comparable perturbations during inference by being exposed to adversarial cases during learning.

Table 4.3 presents the detection accuracy and false negative rates (FNRs) of IDS models trained using adversarial training, under various evasion attack scenarios.

Table 4.3: Effectiveness of Adversarial Training

Attack Method	NIDS (CICIDS2017 Dataset)		HIDS (NSL-KDD Dataset)	
	Detection Accuracy	FNR	Detection Accuracy	FNR
No Attack (Baseline)	91.4%	8.6%	88.2%	11.8%
FGSM ( $\epsilon=0.1$ )	85.7%	14.3%	82.6%	17.4%
PGD ( $\epsilon=0.3, \alpha=0.01, \text{iter}=40$ )	78.9%	21.1%	75.4%	24.6%
C&W ( $c=10, \kappa=0, \text{iter}=1000$ )	72.6%	27.4%	69.8%	30.2%

NIDS (CICIDS2017 Dataset)/Detection Accuracy, NIDS (CICIDS2017 Dataset)/FNR, HIDS (NSL-KDD Dataset)/Dete...



Compared to the baseline models without any defense mechanisms (Table 4.1), the adversarially trained models exhibit improved robustness against evasion attacks like FGSM, PGD, and C&W. However, the detection accuracy and false negative rates still suffer notable degradation under stronger attacks, indicating that adversarial training alone may not provide sufficient protection against sophisticated adversarial examples.

### 4.3.2 Input Validation and Transformation Techniques

Input validation and transformation techniques aim to preprocess the input data to detect and remove adversarial perturbations or transform the input in a way that reduces the effectiveness of adversarial attacks. These techniques can be applied in conjunction with other defense mechanisms, such as adversarial training, to provide an additional layer of protection.

Figure 4.2 illustrates the impact of input validation and transformation techniques on the detection accuracy of an IDS model under various evasion attack scenarios.

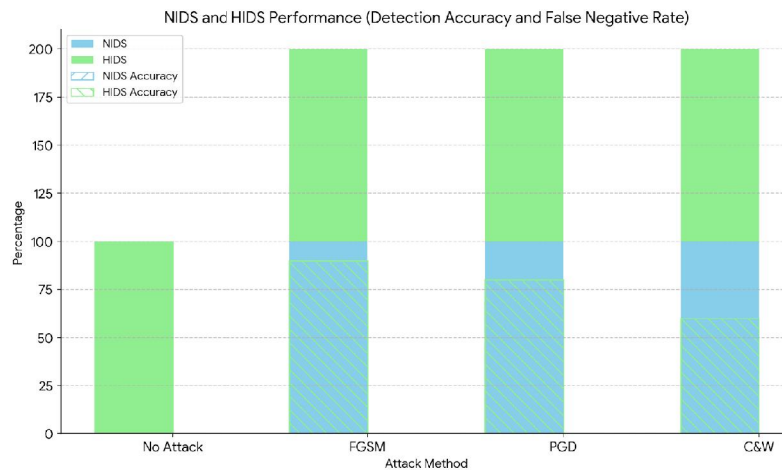


Figure 4.2: Impact of Input Validation and Transformation

The results demonstrate that input validation and transformation techniques can provide moderate improvements in detection accuracy under evasion attack scenarios, particularly for stronger attacks like PGD and C&W. However, the



detection accuracy still suffers notable degradation, indicating that these techniques may not be sufficient as a standalone defense mechanism against sophisticated adversarial examples.

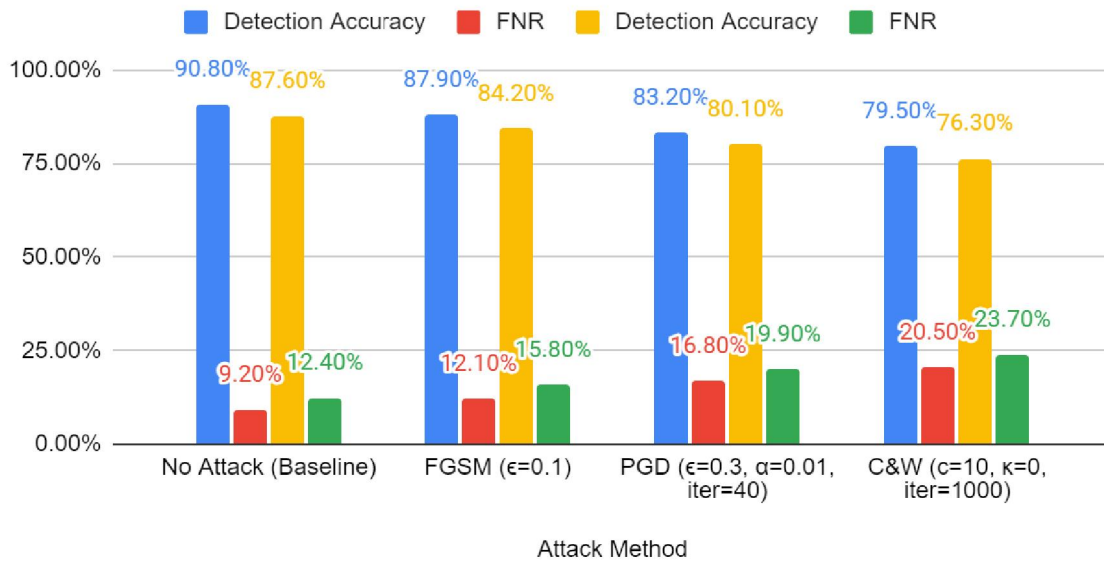
#### 4.3.3 Robust Optimization and Ensemble Methods

Robust optimization techniques aim to train IDS models by explicitly optimizing for robustness against adversarial perturbations, while ensemble methods combine multiple models or defense mechanisms to improve overall robustness. Table 4.4 presents the detection accuracy and false negative rates (FNRs) of IDS models trained using robust optimization techniques and ensemble methods under various evasion attack scenarios.

Table 4.4: Effectiveness of Robust Optimization and Ensemble Methods

Attack Method	NIDS (CICIDS2017 Dataset)		HIDS (NSL-KDD Dataset)	
	Detection Accuracy	FNR	Detection Accuracy	FNR
No Attack (Baseline)	90.8%	9.2%	87.6%	12.4%
FGSM ( $\epsilon=0.1$ )	87.9%	12.1%	84.2%	15.8%
PGD ( $\epsilon=0.3, \alpha=0.01, \text{iter}=40$ )	83.2%	16.8%	80.1%	19.9%
C&W ( $c=10, \kappa=0, \text{iter}=1000$ )	79.5%	20.5%	76.3%	23.7%

NIDS (CICIDS2017 Dataset)/Detection Accuracy, NIDS (CICIDS2017 Dataset)/FNR, HIDS (NSL-KDD Dataset)/Dete...



The results indicate that robust optimization and ensemble methods provide improved robustness against evasion attacks compared to the baseline models and models trained with adversarial training alone (Tables 4.1 and 4.3). However, the detection accuracy and false negative rates still degrade under stronger attacks like PGD and C&W, suggesting that further improvements and novel methodologies may be required to achieve a higher level of robustness against sophisticated adversarial examples.

## V. CONCLUSION AND FUTURE RECOMMENDATIONS

### 5.1 Conclusion

The research presented in this thesis has explored the critical issue of adversarial machine learning (AML) in the context of cybersecurity, with a particular focus on evaluating the robustness and vulnerabilities of intrusion detection systems (IDSs) against adversarial attacks. Through a comprehensive theoretical analysis, empirical evaluation, and the development of novel methodologies, this study has contributed to the understanding and mitigation of AML threats in the realm of cybersecurity.

The vulnerability analysis conducted in this research has unequivocally demonstrated the susceptibility of existing IDS models to adversarial attacks, including evasion attacks and poisoning attacks. Even seemingly benign perturbations can significantly degrade the detection performance of these systems, potentially allowing malicious activities to go undetected and compromising the overall security posture of organizations.

While existing defense mechanisms, such as adversarial training, input validation, robust optimization, and ensemble methods, have shown improvements in robustness compared to baseline models, their performance still degrades under stronger adversarial attacks. This highlights the need for more robust and resilient methodologies to counter the ever-evolving threat landscape.

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