

Progressive Collapse Analysis of Vertical Irregular Steel Structure

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Abstract: The structural engineer's role becomes challenging when such buildings which are irregular in plan as well as in elevation. All these structures are analysed and designed as per Indian standard (IS800:2007, IS1893:2016) with all combination of loading. After that these structures are again analysed for progressive collapse. These types of analysis are considered i.e. linear static and non-linear static with load six case and critical location suggested by GSA guidelines. From this study following observations are made, as height of structure affects the collapse behaviour, as height increases progressive collapse decreases which is seen from D.C.R. values, joint displacement, and bending moment. Linear static analysis results are more conservative than nonlinear static analysis.

Keywords: Progressive collapse

I. INTRODUCTION

Progressive collapse of structures is initiated by the loss of one or more load-carrying members. As a result, the structure will seek alternate load paths to transfer the load to structural elements, which may or may not have been designed to resist the additional loads. Failure of overloaded structural elements will cause further redistribution of loads, a process that may continue until stable equilibrium is reached. Equilibrium may be reached when a substantial part of the structure has already collapsed. The resulting overall damage may be disproportionate to the damage in the local region near the lost member. Loss of primary members and the ensuing progressive collapse are dynamic nonlinear processes.

Progressive collapse implies disproportional global structural system failure originated by local structural damage. It is a rare event, as it necessitates an initiation of local element removal criteria either due to the inevitable forces of nature or due to manmade hazards. The gravity load of the structure is now transferred to neighboring columns; these columns should resist the additional abnormal gravity loads & redistribute loads to avoid failure of the major part of the structure. Present day structure design practices and lesser integral ductility and continuity, gets more prone to progressive collapse. However, there should be certain provisions needed for additional consideration to ascertain the safety of structure after any local failure.

1.1 Background of Progressive Collapse

Progressive collapse is not a new problem for structural engineers, who have always been in some way concerned with the possibility that the loss of load-carrying capacity of a relatively small portion of a structure could lead to a disproportionate level of damage. Following are some examples given in table

Table-1 the past cases of progressive collapse

Year	Description
1968	Roman point apartment newham, east London due to gas explosion
1973	26 story skyline towers building in Fairfax county, Virginia because of premature removal of shoring from beneath newly poured floors.
1985	22 story Wedbush building due to over loading on floors so lead to progressive collapse.
1995	The murrah federal office building in Oklahoma city was destroyed by a

	bomb
2001	World trade Centre tower 1 and 2 collapse due to jetliner crashed with a high speed in a building
2005	28 story Windsor tower in Madrid, Spain suffered the collapse on 11 th floor of the building
2013	8 story rana plaza commercial office complex in saver, Bangladesh due to improper use of building.
2017	Plasco building, Tehran due to fire attack

1.2 Aim

Modelling and analysis of vertical irregularity of steel structure due to progressive collapse

1.3 Objective

- Study of progressive collapse analysis.
- Discuss guidelines for column removals in structure.
- To study the effect of vertical irregularity of steel structure due to progressive collapse
- To find the critical location of removal of column as per GSA guidelines

1.4 Problem statement

There are very few studies of progressive collapse of irregular steel structure. In this study analytical approach concentrated on simulation structural response of three dimensional vertical irregular steel structure models were considered. many guides allows linear static procedures designing against progressive collapse.

In this study of different heights of structure such as 5x7, 7x 9,9x11 stories considered. And analyzed for all combination of loading. And maintain demand capacity of structure between 0.5 to 0.9 which is consider as an economical. Then apply GSA-2013 guide lines and then structure analyzed for progressive collpase.and compare before and after result of DCR, displacement of removal location of column and from which finding the critical location of column

II. METHODOLOGY

This chapter describes the various methods approaches used for analysis and design of steel structure. This structure provided with material and section properties for column and beams. Presented below. The details of modelling of irregular structure such as 5x7,7x9,9x11 story structure and location of column removal at different level for progressive collapse are discussed.

Design Methodology

our study is based analysis of vertical irregular steel frame structure such as 5x7,7x9,9x11 for on progressive collapse, considering sudden loss of column as a design scenario and the structure analysis for effect of vertical irregularity on progressive collapse that there are many codes and guideline available worldwide but most of the research work uses the GSA guideline

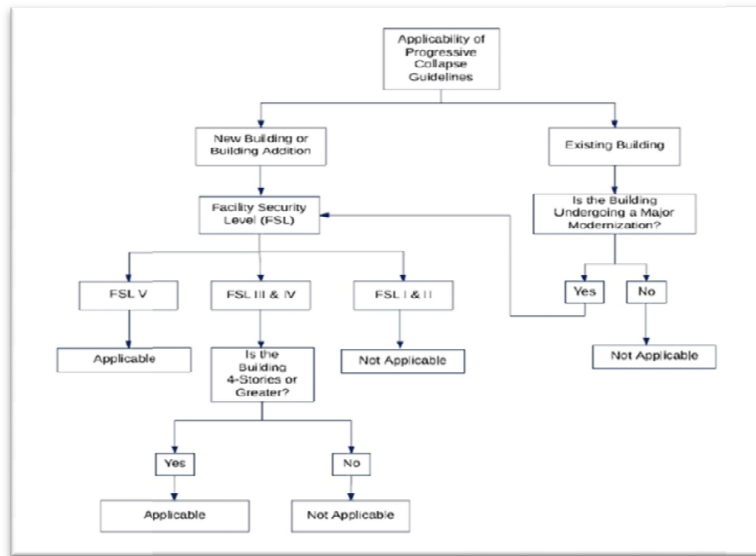


Figure 1: location of external column removal

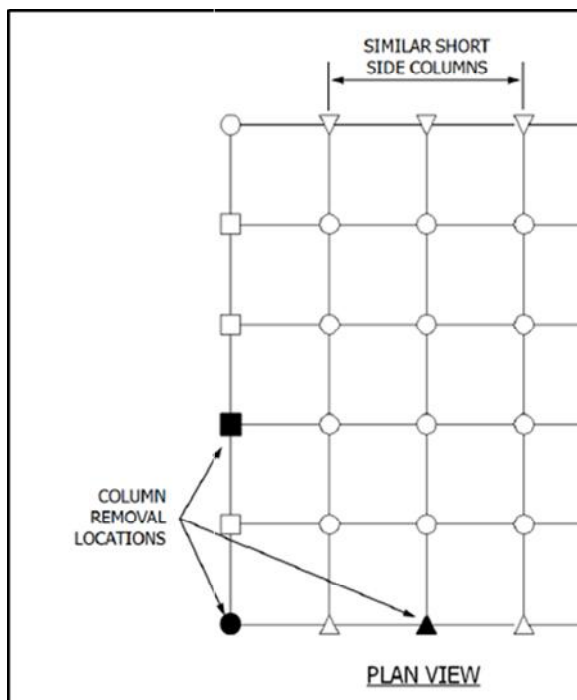


Figure 1: location of external column removal

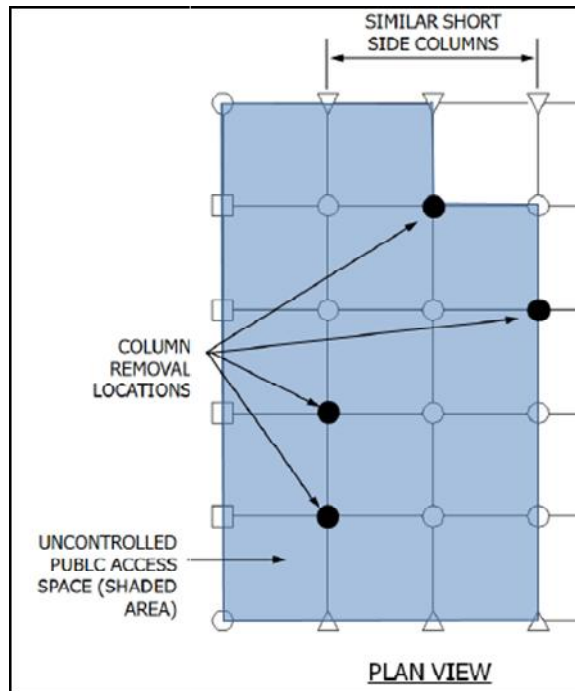


Figure 3: location of external column removal

Design procedure of progressive collapse.

For our research work there are various methods to analyse the structures and investigate their response to the progressive collapse phenomenon, these methods vary extensively in respect to time consumption and the structural knowledge required to perform the analysis.

We use the latest GSA-2013 for further guideline. The main aim is to reduce progressive collapse over the loss of a structural element, limiting the extent of damage to a localised area and redundant and balance structural system along the height of building.

The most common analysis methods have been used to explore the general structural behaviour in order of increasing complexity are linear static procedure (lsp), linear dynamic procedure (ldp), nonlinear static procedure (nsp), and nonlinear dynamic procedure (ndp). several researchers in the realm of progressive collapse examined the advantages and drawbacks of the different analysis methods in terms of time and accuracy.

Linear static method:

Linear static procedure is very effective for less than or equal to 10 stories. There are two cases deformation control can be calculated by using case i and force control action will be calculated by using case ii. For ductile actions' analysis, the applied load is increased through the use of an lif that considers dynamic and nonlinear effects both. Linear static model, which has one removed column, wall section or another load-bearing member, Irregularity limitations

A structure is considered irregular if any one of the following is true:

1. Significant discontinuities exist in the gravity-load carrying and lateral force-resisting systems of a building, including out-of-plane offsets of primary vertical elements, roof "belt-girders", and transfer girders (i.e., non-stacking primary columns or load-bearing elements). Stepped back stories are not considered an irregularity.
2. At any exterior column except at the corners, at each story in a framed structure, the ratios of bay stiffness and/or strength from one side of the column to the other are less than 50%. Three examples are; a) the lengths of adjacent bays vary significantly, b) the beams on either side of the column vary significantly in depth and/or strength, and c) connection strength and/or stiffness vary significantly on either side of the column (e.g., for a steel frame

Building, a shear tab connection on one side of a column and a fully rigid connection on the other side shall be considered irregular).

3. For all external load-bearing walls, except at the corners, and for each story in a load-bearing wall structure, the ratios of wall stiffness and/or strength from one side of an intersecting wall to the other are less than 50%.

4. The horizontal lateral-load resisting elements are not parallel to the major orthogonal axes of the lateral force-resisting system, such as the case of skewed or curved moment frames and loadbearing walls.

Loading cases for linear static method:

As per mention in paragraph in 3.3.1 there are two cases which are mention below.

Case i: deformation control action qud

$$G_{ld} = \omega_{ld} [1.2 d + (0.5 l \text{ or } 0.2 s)]$$

Where

G_{ld} = increased gravity loads for deformation-controlled actions for linear static analysis

D = dead load including façade loads (lb/ft² or kn/m²)

L = live load including live load reduction, not to exceed the maximum of 50-lb/ft² or 244-kn/m²

S = snow load (lb/ft² or kn/m²)

Ω_{ld} = load increase factor for calculating deformation- controlled actions for linear static analysis; use appropriate value for framed or load-bearing wall structures.

Case ii: force control action quf

$$G_{lf} = \omega_{lf} [1.2 d + (0.5 l \text{ or } 0.2 s)]$$

G_{lf} = increased gravity loads for force-controlled actions for linear static analysis

Ω_{lf} = load increase factor for calculating force-controlled actions for linear static analysis; use appropriate value for framed or load-bearing wall structures

Table 2 : dynamic increasing factor for lsp

Material	Structure type	Ω_{ld} , deformation-controlled	Ω_{lf} , force-controlled
Steel	Framed	0.9 mlif + 1.1	2.0
Reinforced concrete	Framed	1.2 mlif + 0.80	2.0
	Load-bearing wall	2.0 mlif	2.0
Masonry	Load-bearing wall	2.0 mlif	2.0
Wood	Load-bearing wall	2.0 mlif	2.0
Cold-formed steel	Load-bearing wall	2.0 mlif	2.0

Acceptance criteria for lsp

Acceptance criteria are classified on type of component i.e. primary & secondary. Thereafter classifications are made on the basis of actions controlling them i.e. deformation-controlled or force-controlled.

Force controlled action: $\phi Q_{CL} \geq Q_{UF}$

Deformation controlled action: $\phi m Q_{CE} \geq Q_{UD}$

Nonlinear static method:

Once the nonlinear model, both materially and geometrically, is made, the loads are increased with a dynamic increase factor (dif) that takes into account the inertia effects only. The consequent load is then applied to the model when the column is eliminated. The preferred performance level indicates the deformation limits which are compared with the consequent member deformation from deformation- controlled actions. However, in the case of force controlled actions, modification of member strength does not occur. This member strength is compared with the maximum internal member forces (actions).

To model, analyze, and evaluate a building, employ a three-dimensional assembly of elements and components. Create one model for either framed or load-bearing wall structures, respectively. Inclusion of secondary components in the

model is optional. However, if the secondary components are omitted, they must be checked after the analysis, against the allowable deformation-controlled criteria.

Include the stiffness and resistance of primary components. Note that the strength reduction factors are applied to the nonlinear strength models of the deformation controlled components (e.g., the nominal flexural strength of a beam or connection is multiplied by the appropriate ϕ factor). Analyze the model for the nonlinear static load case. Use the stiffness requirements of asce 41 [10] chapters 5 through 8 to create the model. Discretize the load-deformation response of each component along its length to identify locations of inelastic action. The force-displacement behavior of all components shall be explicitly modeled, including strength degradation and residual strength, if any. Model a connection explicitly if the connection is weaker or has less ductility than the connected components, or the flexibility of the connection results in a change in the connection forces or deformations greater than 10%. If there is any possibility that the presence of the short section will affect the taller section in a negative manner.

To calculate the deformation-controlled and force-controlled actions, simultaneously apply the following combination of gravity loads:

Increased gravity loads for floor areas above removed column or wall.

Apply the following increased gravity load combination to those bays immediately adjacent to the removed element and at all floors above the removed element.

$$G_n = \Omega_n [1.2 d + (0.5 l \text{ or } 0.2 s)]$$

Where, G_n = increased gravity loads for nonlinear static analysis

D=dead load

S= snow load

Ω_n = dynamic increase factor for calculating deformation-controlled and force controlled actions for nonlinear static analysis.

Gravity loads for floor areas away from removed column or wall. Apply the gravity load combination in below equation to those bays not loaded with g_n

$$G = 1.2 d + (0.5 l \text{ or } 0.2 s)$$

For those bays not immediately adjacent to there moved element the load combination is the same for both deformation and force- controlled action.

Dynamic increasing factor:

The nonlinear static dynamic increase factors (Ω_n) are provided in table below par is the plastic rotation angle given in the acceptance criteria tables in asce 41 [10] and this document for the appropriate structural response level (collapse prevention or life safety for the particular element, component or connection;

θ_y is the yield rotation. For steel, θ_y is given in equation 5-1 in asce 41 [10]. For reinforced concrete, θ_y is determined with the effective stiffness values provided in table 6-5 in asce 41 [10]. Note that for connections, θ_y is the yield rotation angle of the structural element that is being connected (beam, slab, etc) and θ_{pra} is for the connection(determined from asce 41 [10]). Columns are omitted from the determination of Ω_n to determine Ω_n for the analysis of the entire structure, choose the smallest ratio of θ_{pra}/θ_y for any primary element, component, or connection in the model within or touching the area that is loaded with the increased gravity low

Table 3: dynamic increase factors (Ω_n) for nsp

Material	Structure type	Ω_n
Steel	Framed	$1.08 + 0.76/(\theta_{pra}/\theta_y + 0.83)$
Reinforced concrete	Framed	$1.04 + 0.45/(\theta_{pra}/\theta_y + 0.48)$
	Load-bearing wall	2.0
Masonry	Load-bearing wall	2.0
Wood	Load-bearing wall	2.0
Cold-formed steel	Load-bearing wall	2.0

III. MODELLING AND ANALYTICAL STUDY

Theoretical model selected for the study of progressive collapse having symmetrical base with vertical irregularity of 3x5, 5x7, 7x9, 9x11 is steel structure building. The structure consists of seven bays of 4 m in the longitudinal direction and seven bays of 4 m in the transverse direction

Detail description of model is given in table.

Table 4: Description of model

Sr.no.	Particulars	Description
1	Type of structure	Moment resisting frame
2	Type of building	Commercial building
3	Number of stories	5x7,7x9,9x11
4	Height of building	3 meter
5	Spacing in x direction	5 meter
6	Spacing in y direction	5 meter
7	Material	Fe345,fe250,m25(concrete)
8	Thickness of slab	150 mm thk
9	Codal provision	Is 800:2007,is1893:2002

Table 5:loading data for structure:

Sr. no.	Particulars	Description
1	Dead load	Self-weight of structure
2	Live load	2.5 kn/m ²
3	Floor finish	1.25kn/m
4	wall load	10kn
5	Wall load on roof	3kn
6	Seismic load	Is1893:2002
6.a	Importance factor	1
	Zone	Iii
	Soil type	Medium
	Type of structure	Special moment resisting frame
	Response reduction factor	5

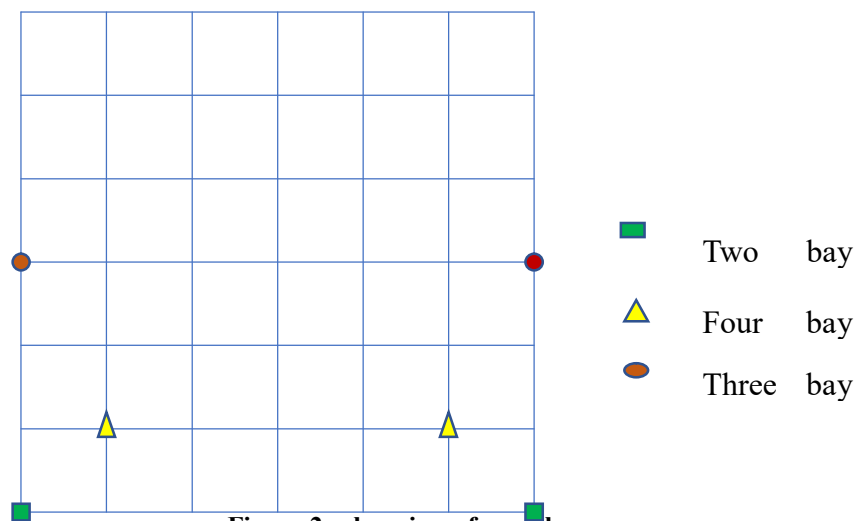


Figure 2: plan view of models

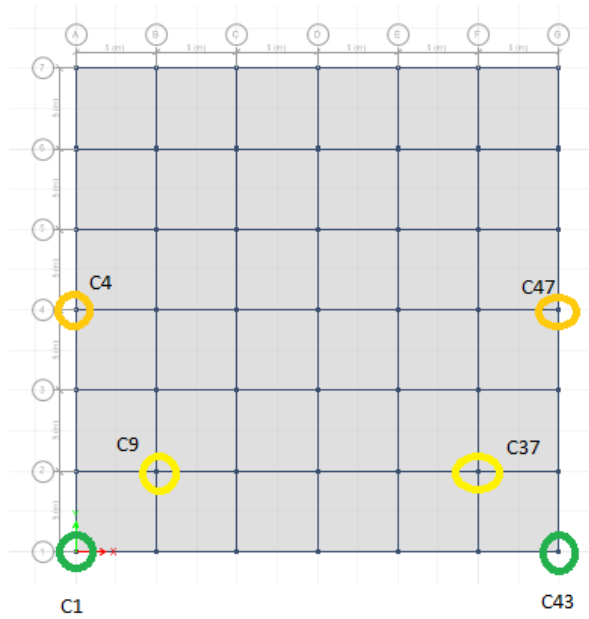


Figure 3: plan view of removal of location of column

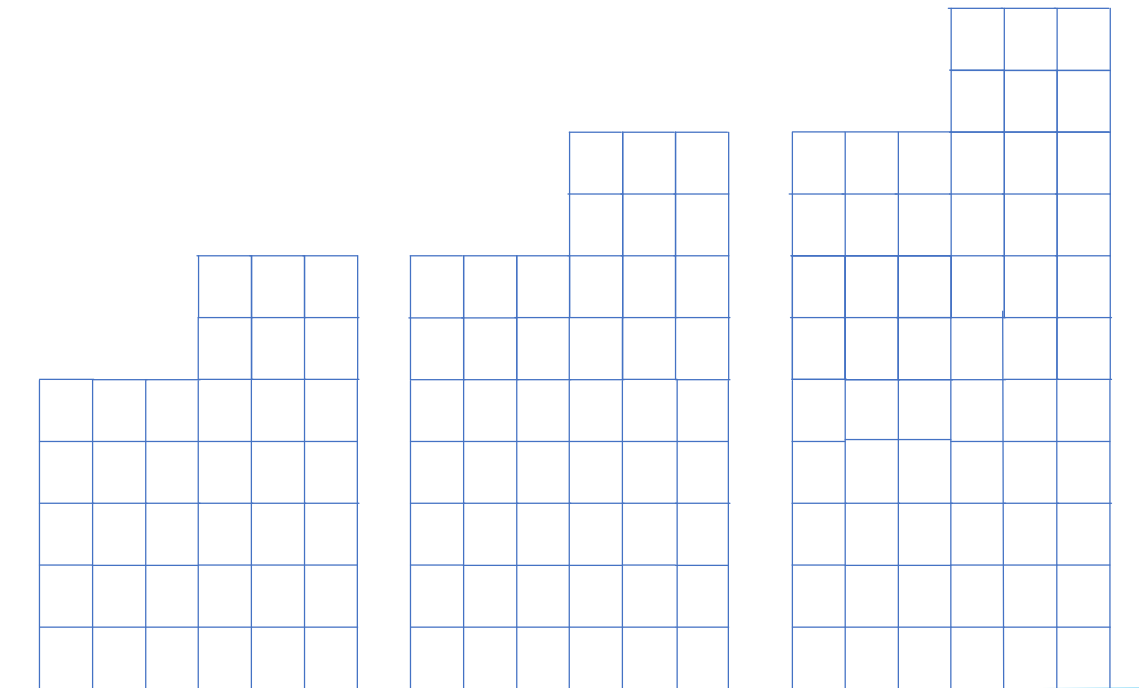


Figure 4: elevation view of 2d models

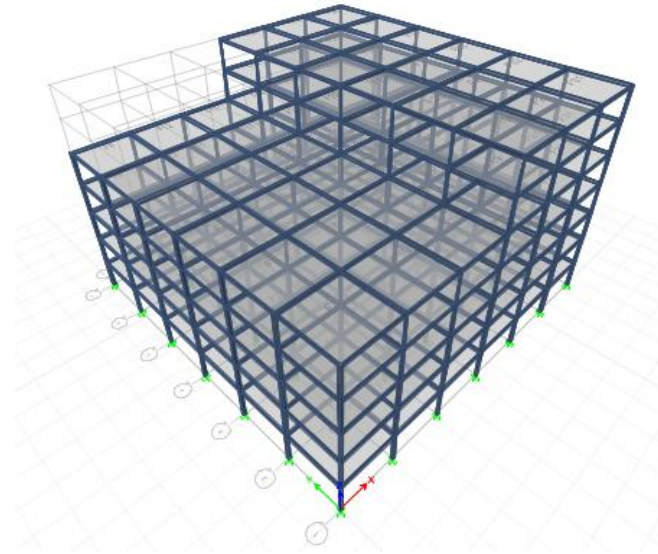


Figure 5: elevation view of 3d models

IV. RESULT AND DISCUSSION

This chapter basically deals with presentation of results obtained until & graphs plotted using the same. Their interpretation is also done after the results to understand the actual behaviour of progressive collapse of steel framed structures.

The linear elastic static analysis using etabs 2015 bending moment diagram, shear force, axial force in beams, column axial force, demand capacity ratios and joint displacement is obtained, the DCR values for member under consideration loaded with GSA code of practice is worked out to know the behaviour of columns and beams in the structure.

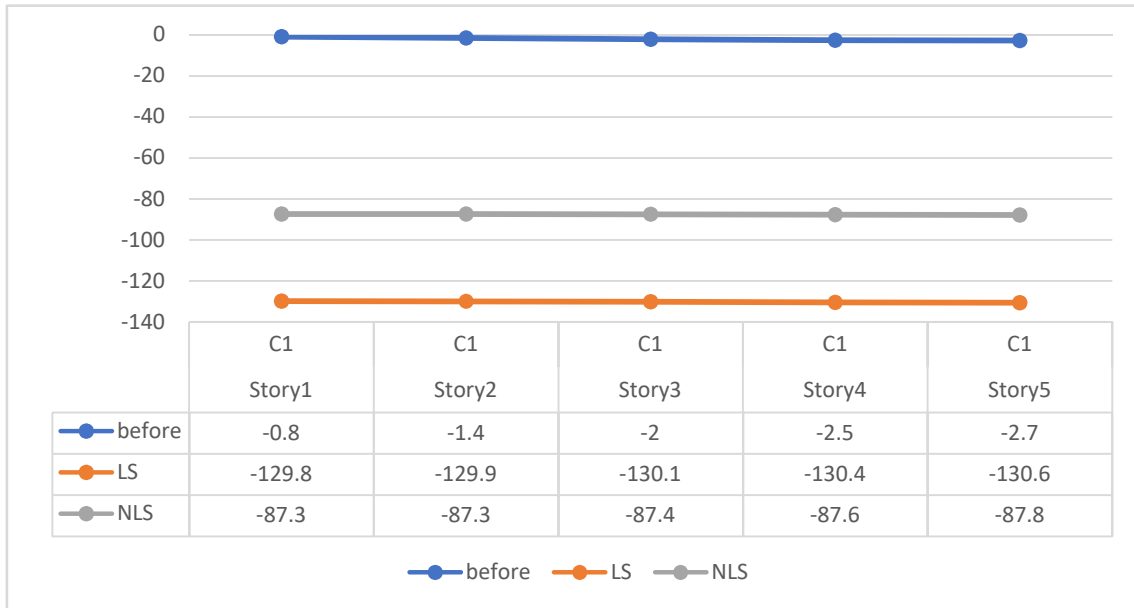
For all models such as 5x7,7x9,9x11 following load cases are considered for linear static and nonlinear static

- Case i : location of column removal no. 1
- Case ii : location of column removal no. 4
- Case iii : location of column removal no. 9
- Case iv : location of column removal no.37
- Case v : location of column removal no.43
- Case vi : location of column removal no.47

Results and graphs for all models

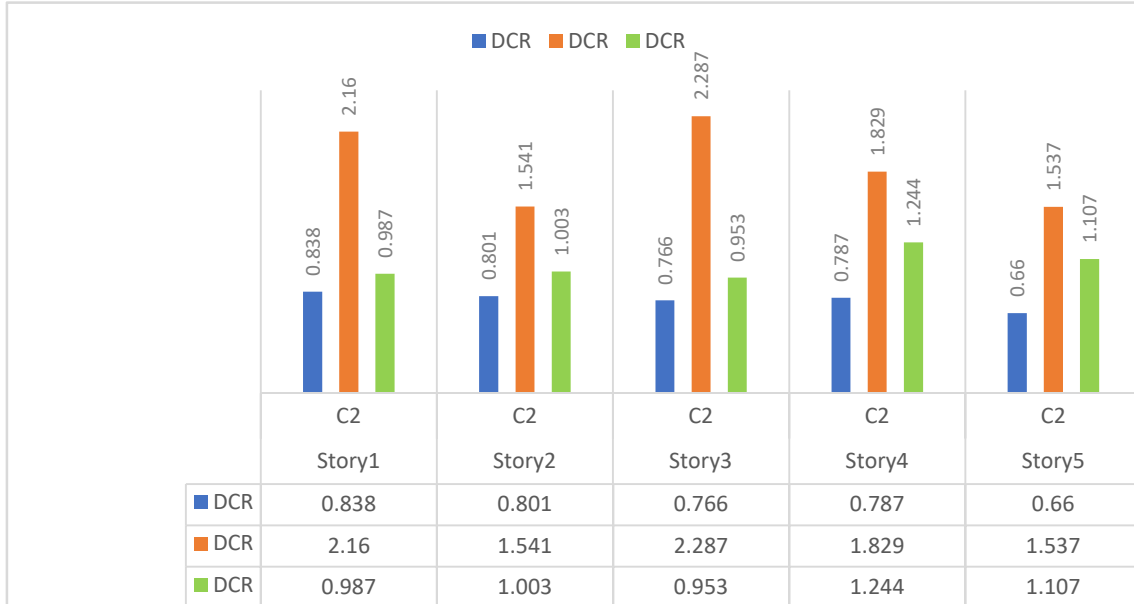
In progressive collapse analysis through linear static analysis and nonlinear static analysis has been observed the various parameters to study behaviour of structures in such abnormal events.

**Graph 1: displacement DCR ,bending moment for column no. 1(5x7)
Joint displacement for column no.c1**

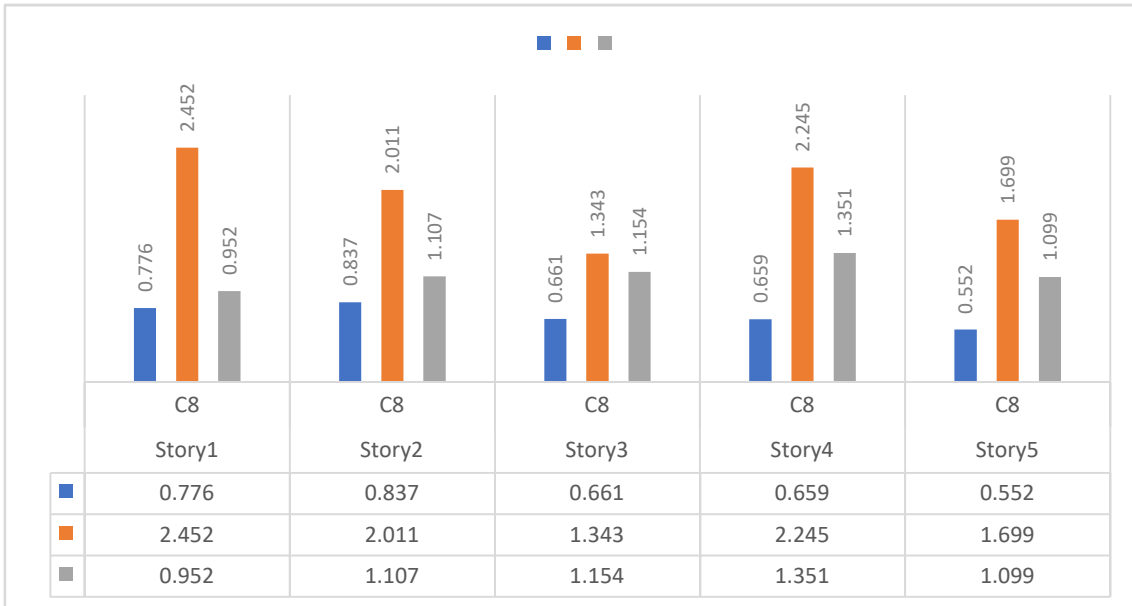


This graph shows displacement behavior of structure before removal of column and after removal of column for linear static and nonlinear static. The nonlinear static displacement is less due to less amplification factor is used for nonlinear static analysis.

Demand capacity ratio of column after removal of c2

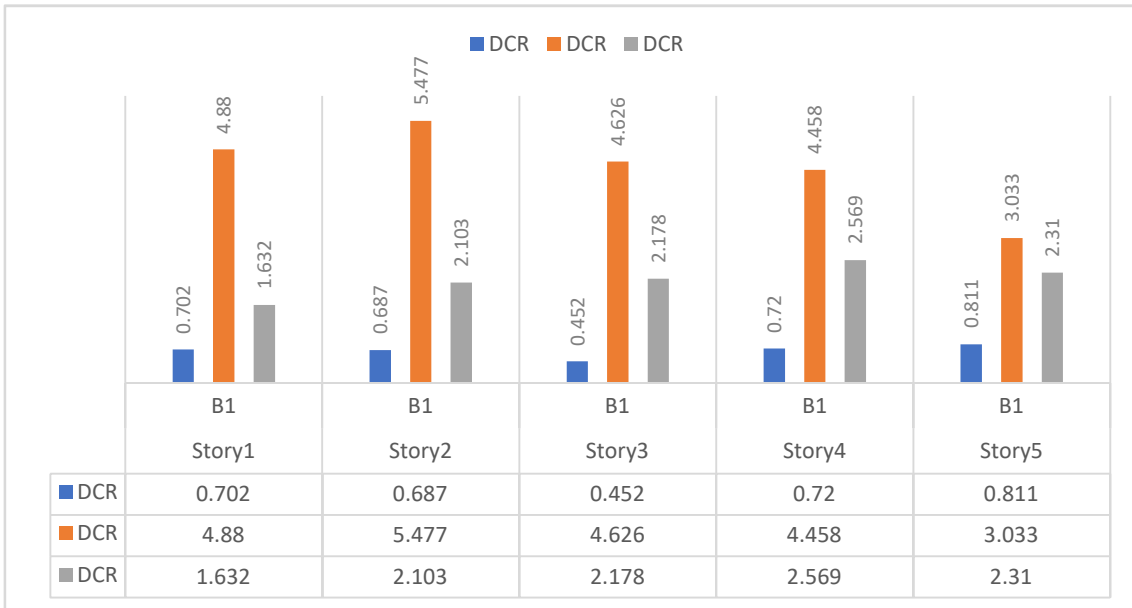


The graph shows for original structure D.C.R. values are within the limit i.e.less than 0.9 but linear static column removal case values are larger at ground floor and reduces to top story. As compare to nonlinear static analysis.

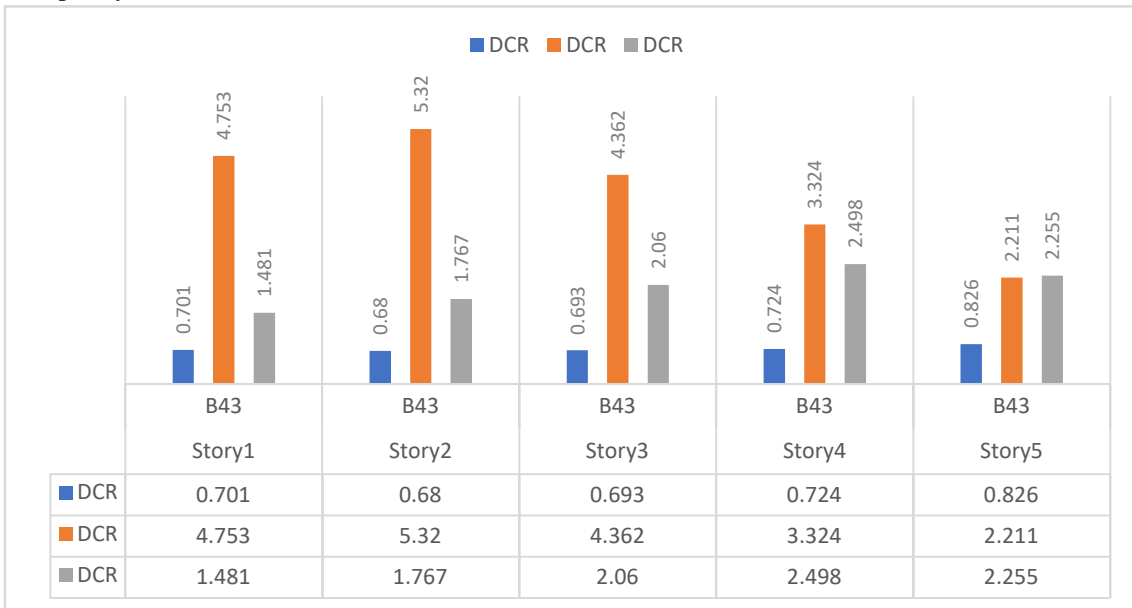


The graph shows for original structure D.C.R.values are in between 0.5 to 0.9 but linear static column removal case values are larger at ground floor is 2.452 and reduces to top story is 1.699.as compare to nonlinear static values.

Demand capacity ratio of beam no b1

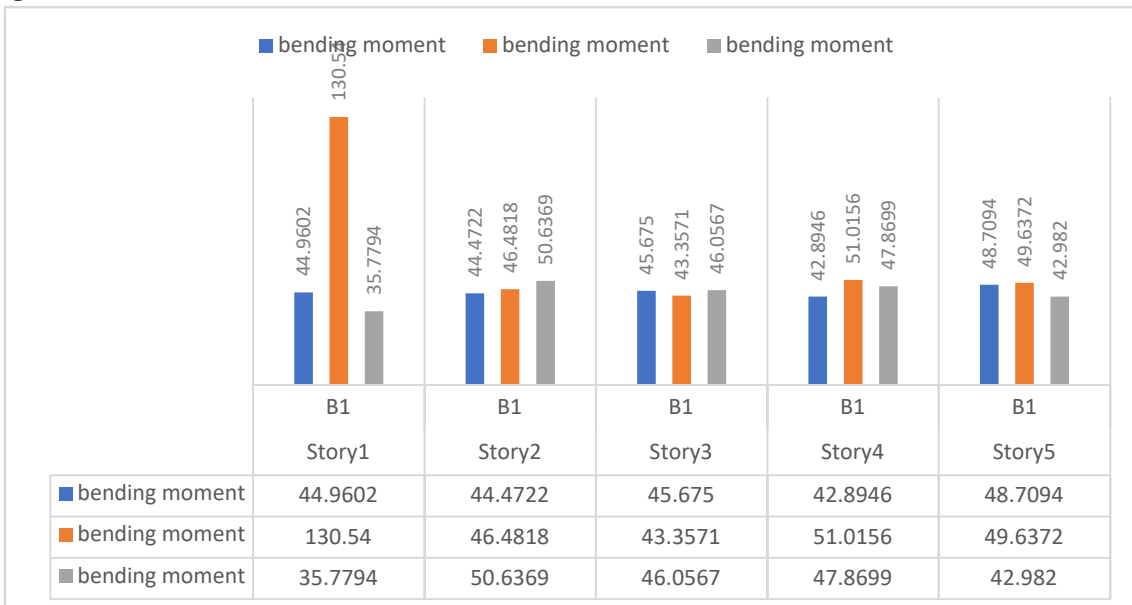


Demand capacity ratio of beam no b43

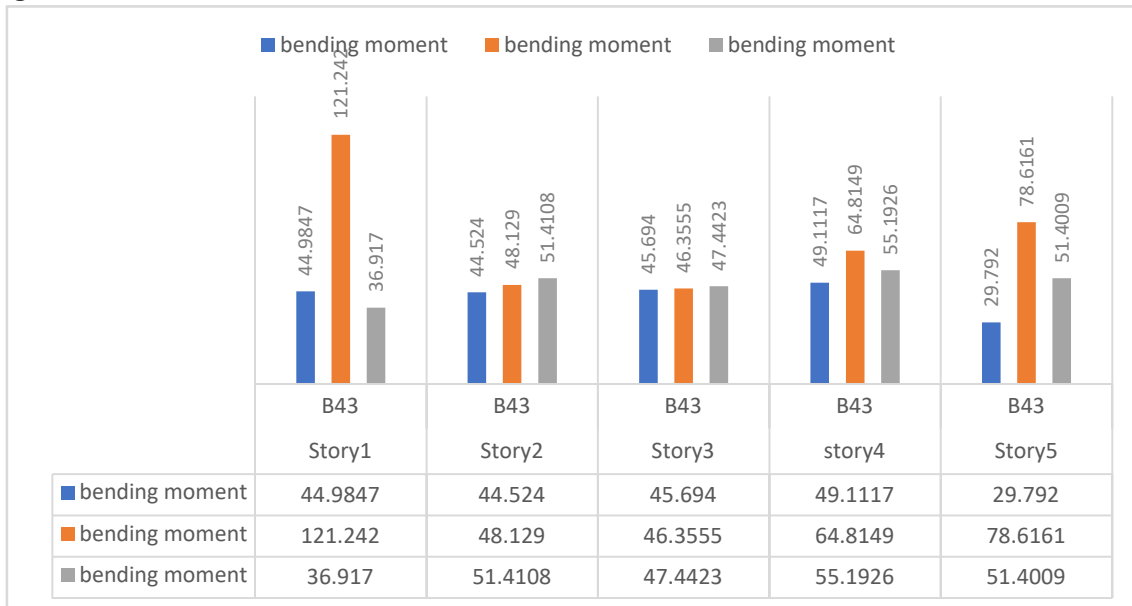


Graph shows large increasing in DCR value in beam because beam no1 and beam no.43 has not transfer the load to adjacent column because of removal column no.c1

Bending moment of beam no 1



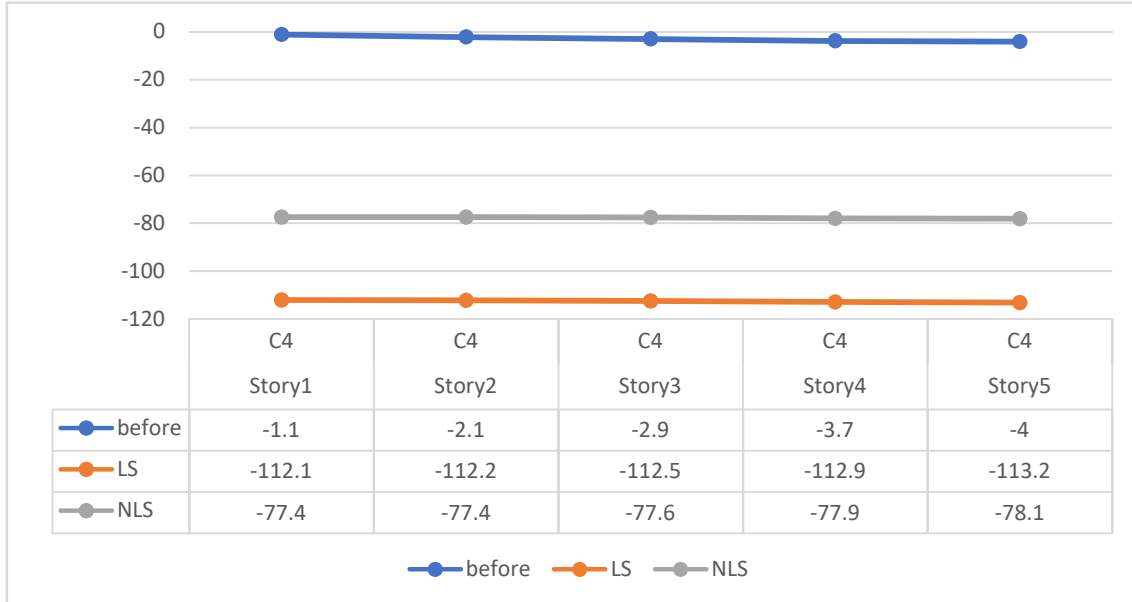
Bending moment of beam no 43



The bending moment values for beam no b1 and b43 are abruptly changes when removal of column c1 as compare to original structure this is seen maximum at ground story than other stories.

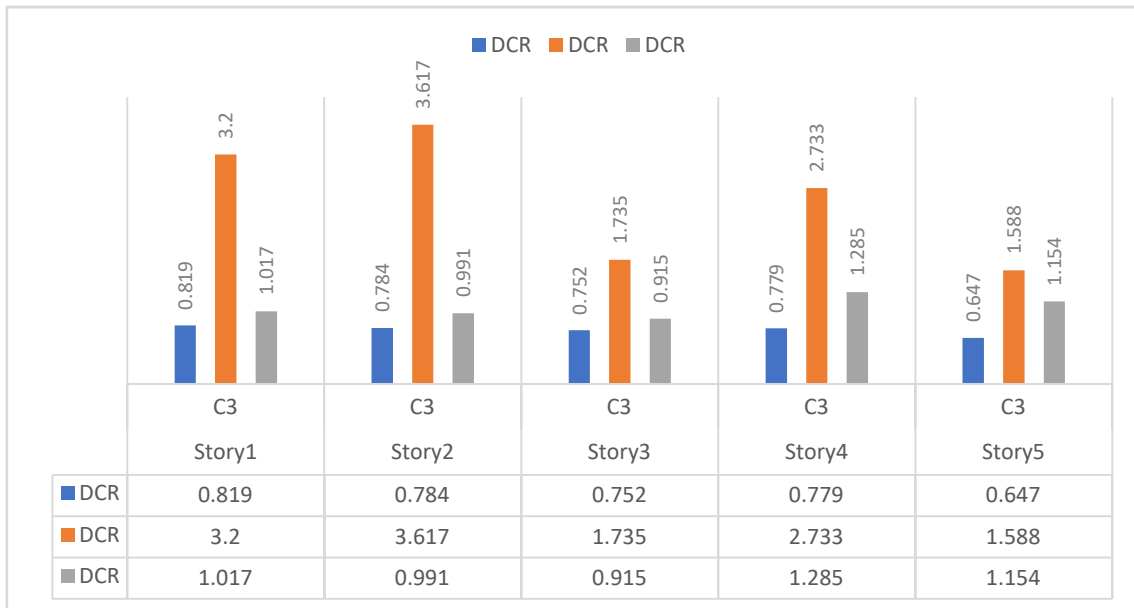
Graph 2:displament, DCR ,bending moment for column no 4(5x7)

Joint moment displacement for c4

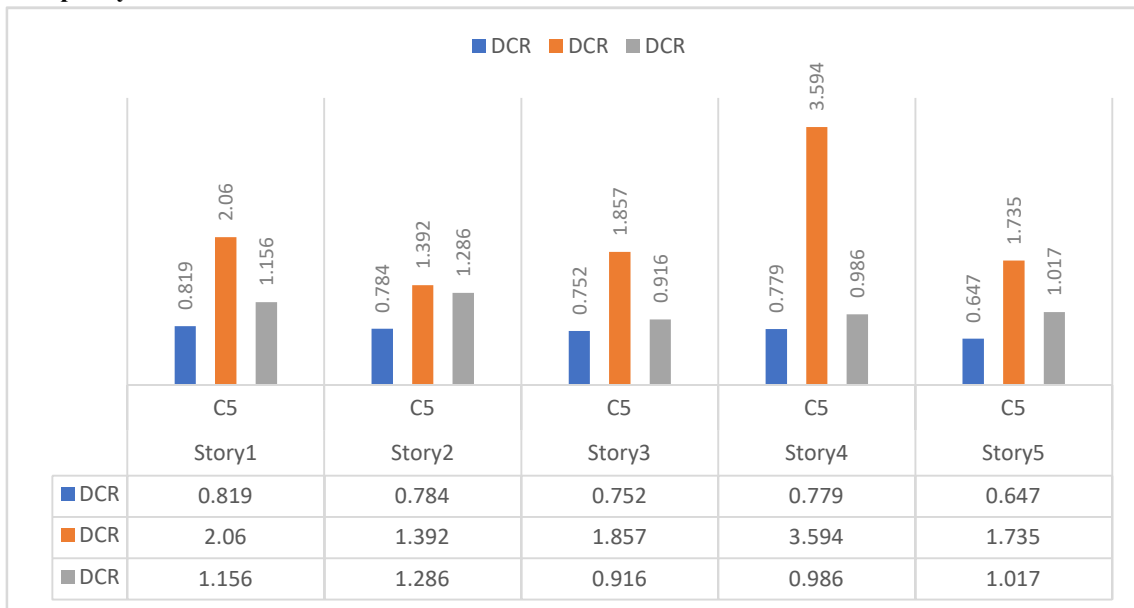


This graph shows displacement behavior of structure before removal of column and after removal of column for linear static and nonlinear static. The nonlinear static displacement is a reduced amount of due to less amplification factor is used for nonlinear static analysis.

Demand capacity ratio for the column no c3

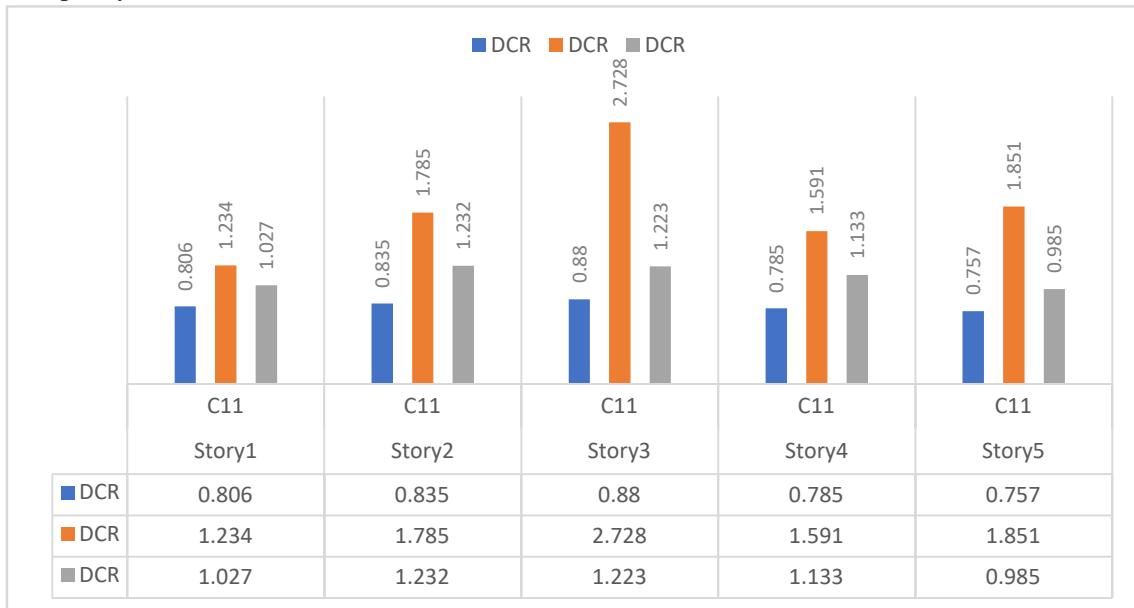


Demand capacity ratio for the column no c5

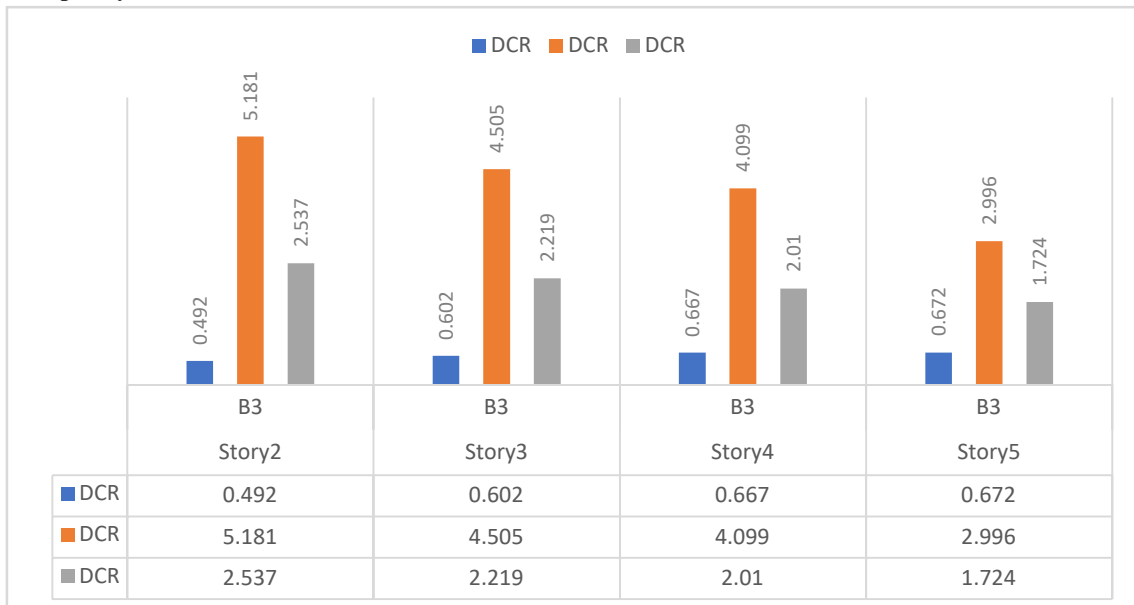


The graph shows for original structure D.C.R.values but linear static column removal case values are larger at ground floor is 3.2 for c3 and 2.05 for c5 and reduces to top story is 1.154 for c3 and 1.735 for c5.as compare to nonlinear static values.

Demand capacity ratio for the column no c11

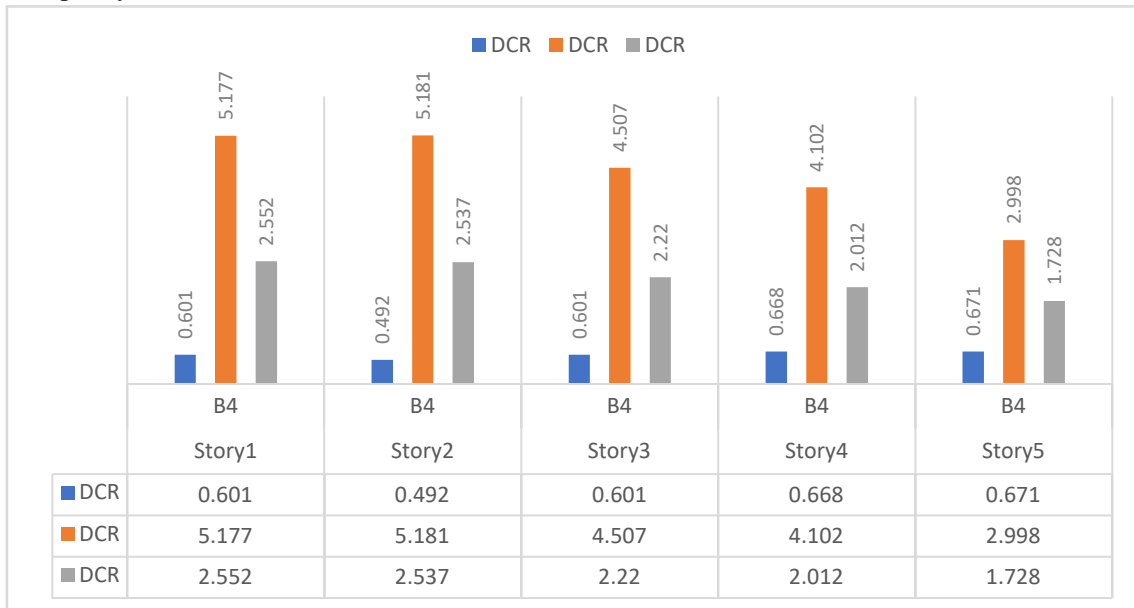


Demand capacity ratio for beam no b3:

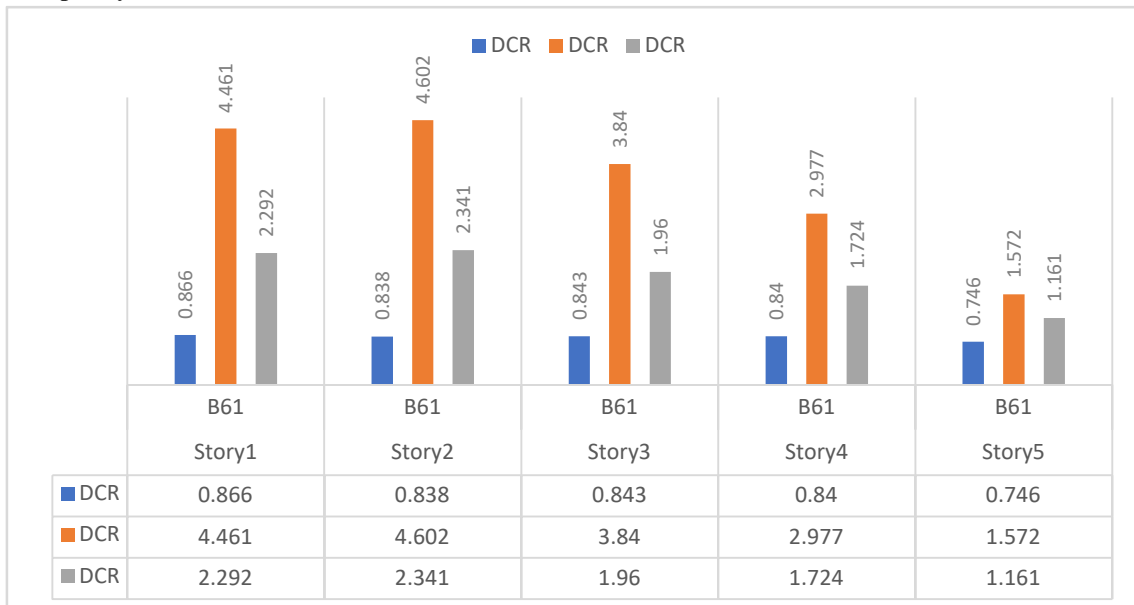


Graph shows large increasing in DCR value in beam because beam no3 has more value on ground floor is 5.181 which is reducing at top floor is 2.996 for linear static than nonlinear static

Demand capacity ratio for beam no b4:

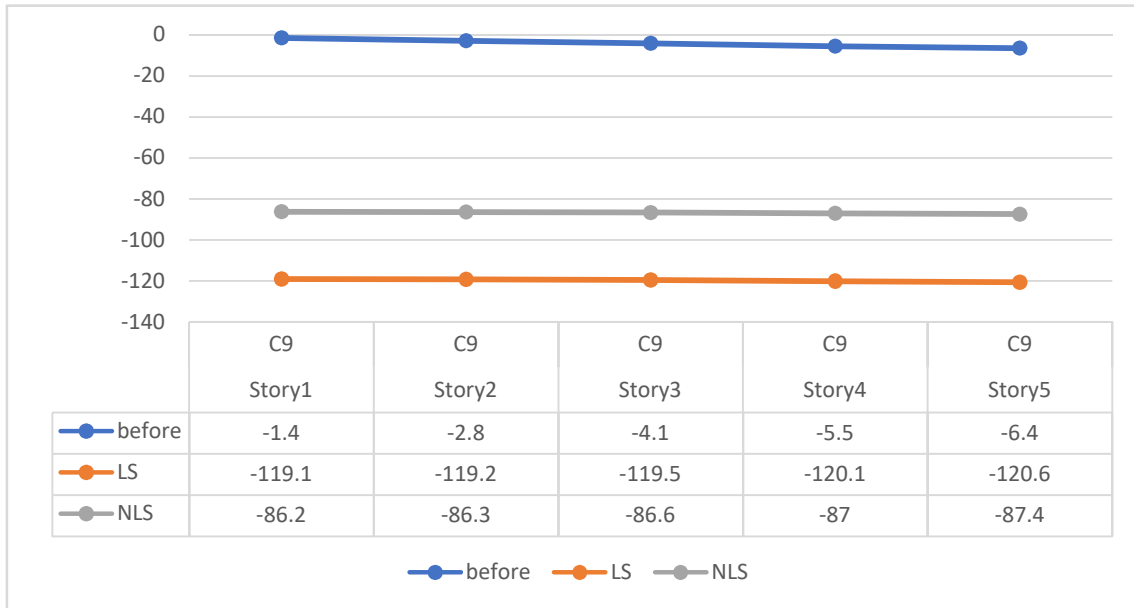


Demand capacity ratio for beam no b61:



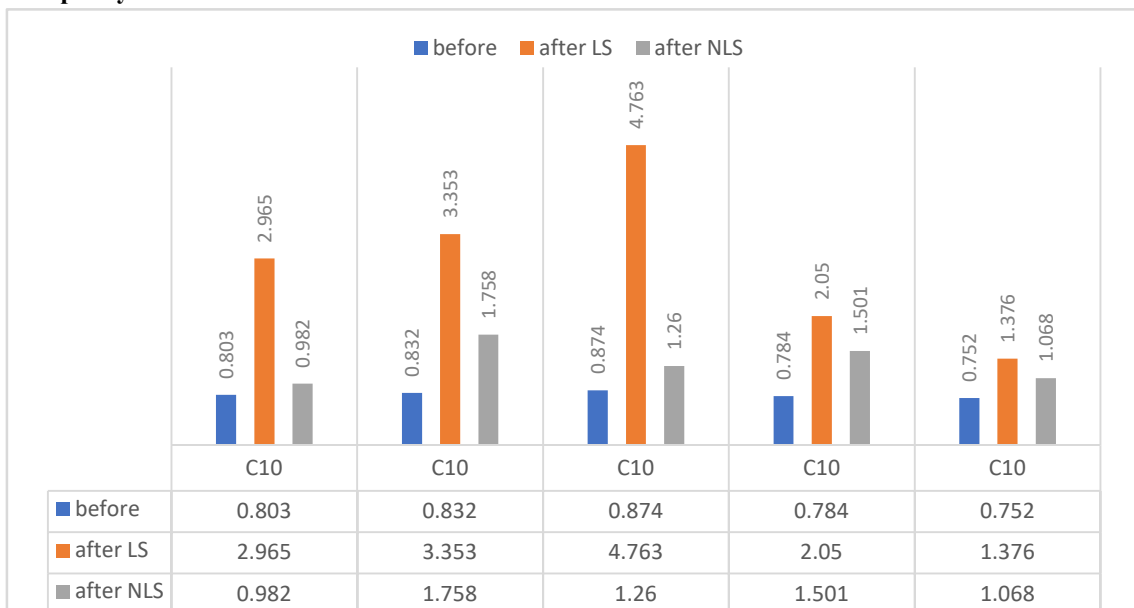
Graph shows large increasing in DCR value in beam because beam no.4 has not transfer the load to adjacent column because of removal column no.c4

**Graph 3:displacement, DCR ,bending moment for column no. 9 (5x7)
Joint displacement for column no.c9**



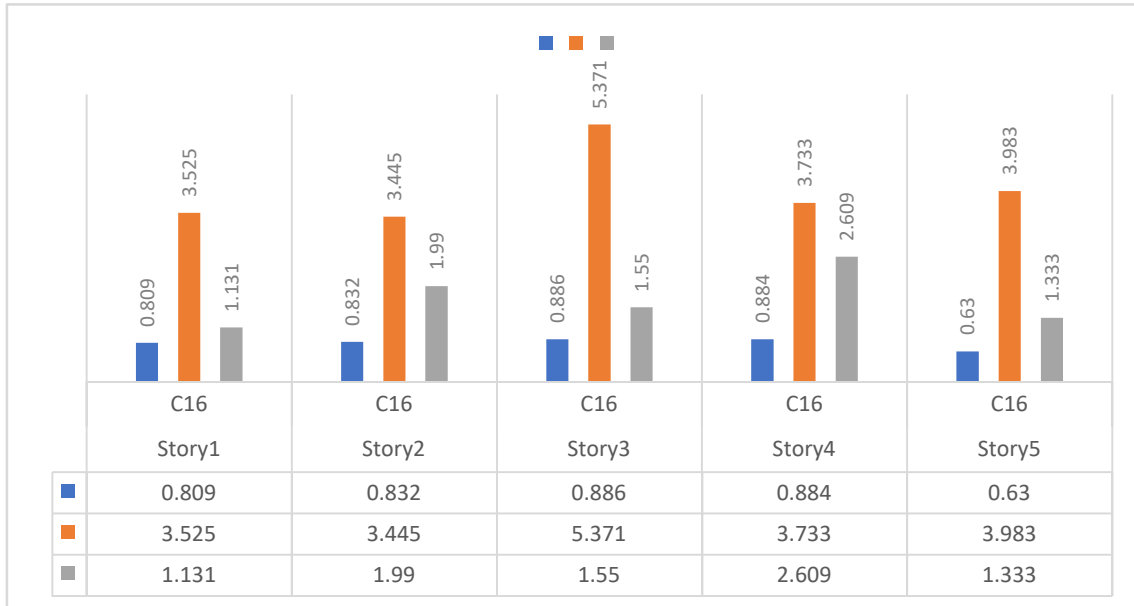
Results shows that for displacement for column c9 before removal of column increases gradually as story goes on increasing but for linear static case values are more than nonlinear static case because amplification factor is large.

Demand capacity ratio for the column no c10



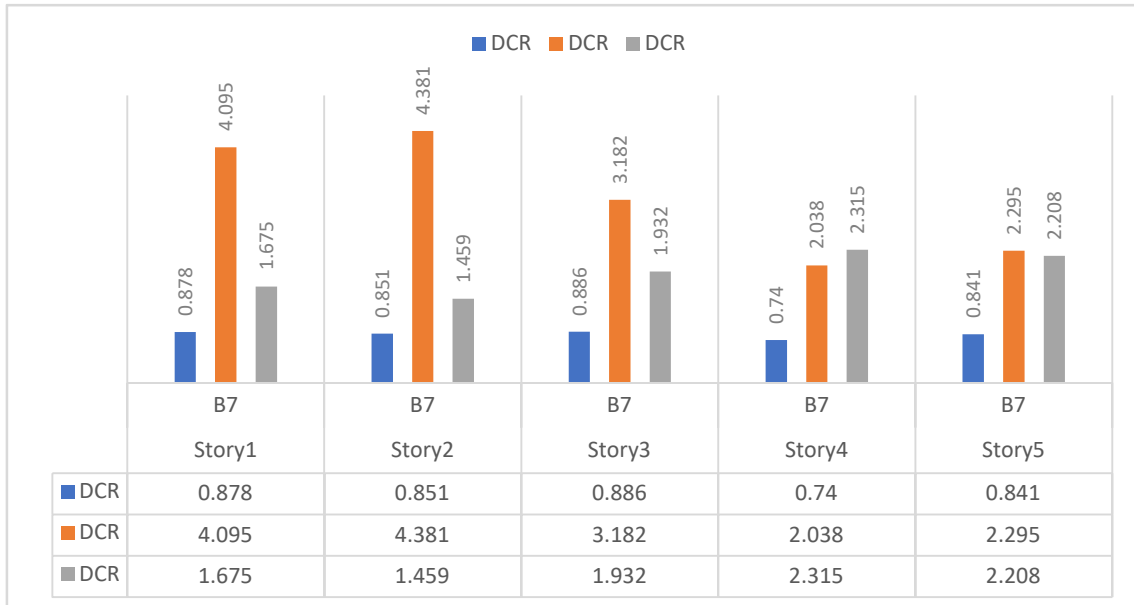
The graph shows that d.c.r. values for before removal of column is in between 0.7 to 0.85but for after removal of location the values are suddenly increases at ground story is 2.965 and goes on reducing to 1.376 as compared to nonlinear static analysis.

Demand capacity ratio for the column no c16

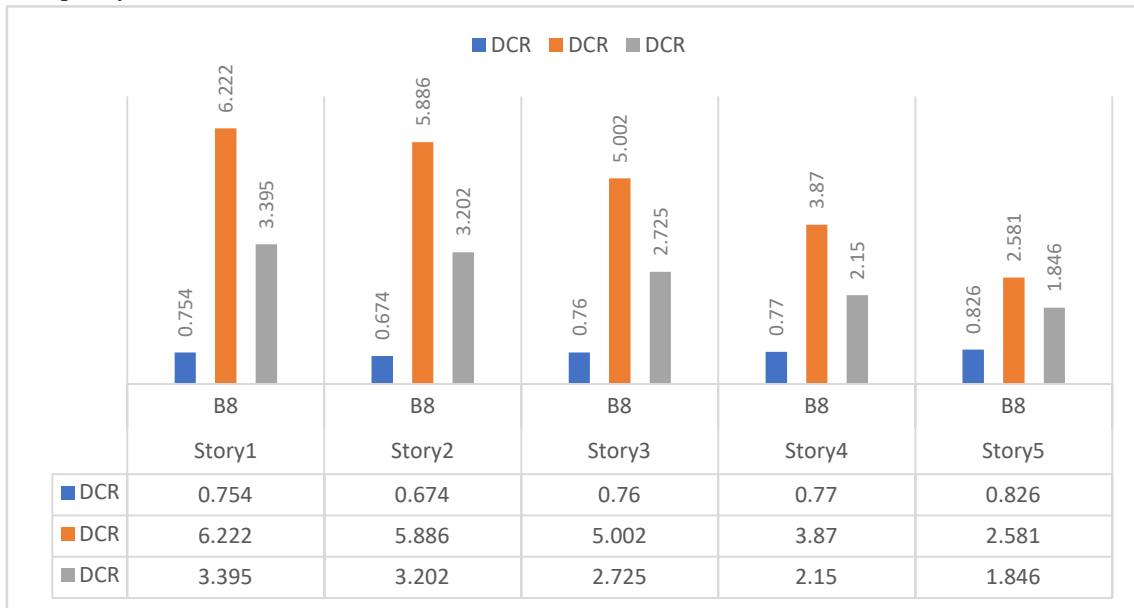


The graph shows for original structure D.C.R.values are in between 0.5 to 0.9 but linear static column removal case values are larger at ground floor and reduces to top story is .as compare to nonlinear static values.

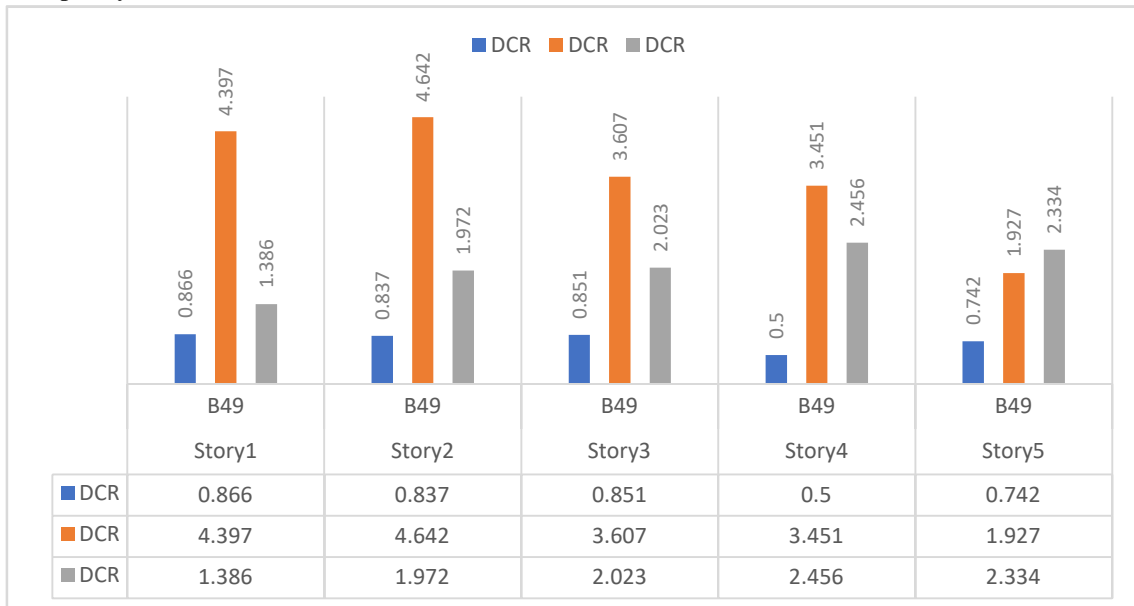
Demand capacity ratio for the beam no b7



Demand capacity ratio for the beam no b8

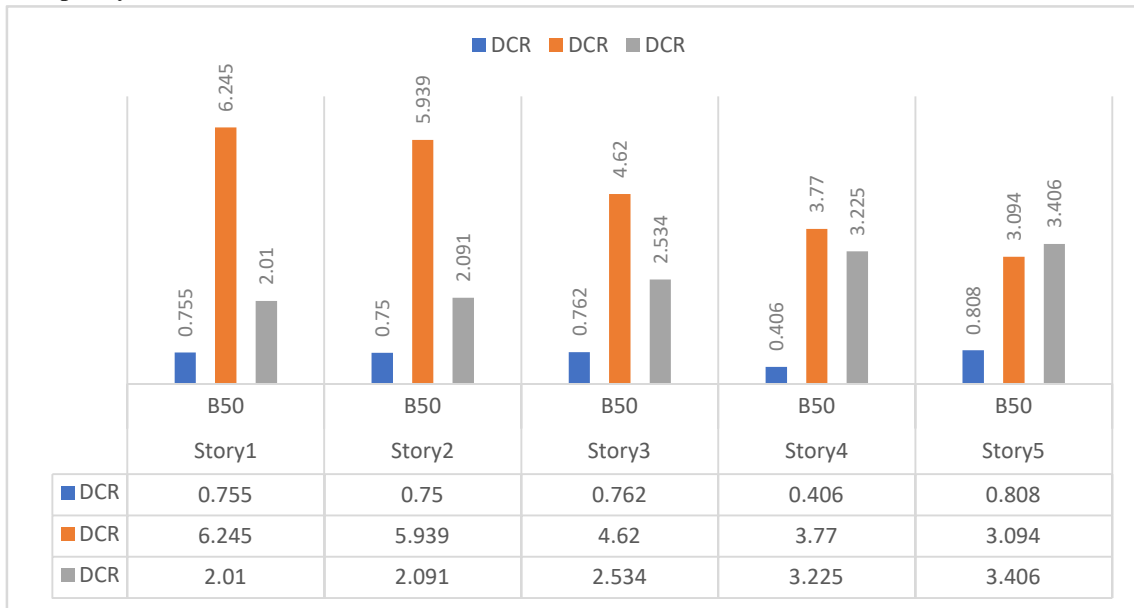


Demand capacity ratio for the beam no b49



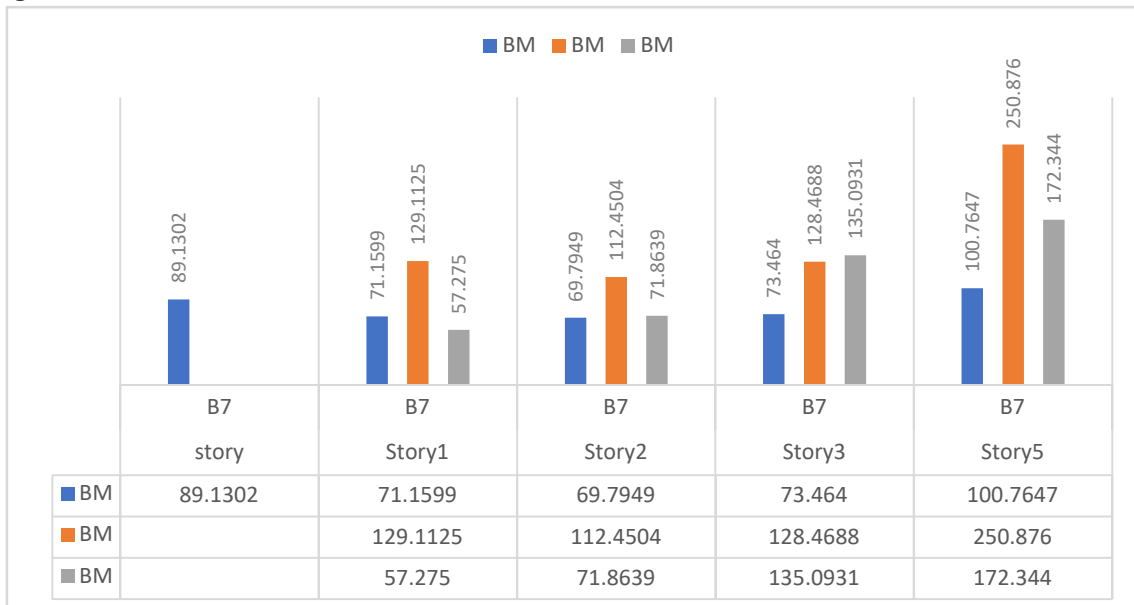
Above all graph shows that for original structure D.C.R.values are in between 0.5 to 0.9 but linear static column removal case values are larger at ground floor and reduces to top story is .as compare to nonlinear static values.

Demand capacity ratio for the beam no b50

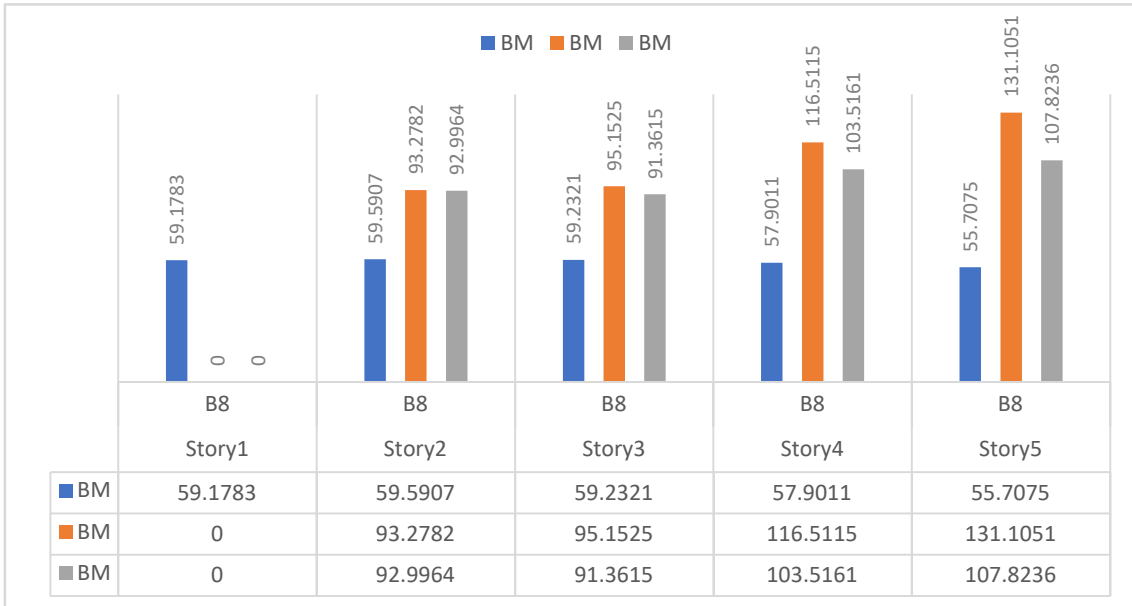


Above all graph shows that for original structure D.C.R.values are in between 0.5 to 0.9 but linear static column removal case values are larger at ground floor and reduces to top story is .as compare to nonlinear static values.

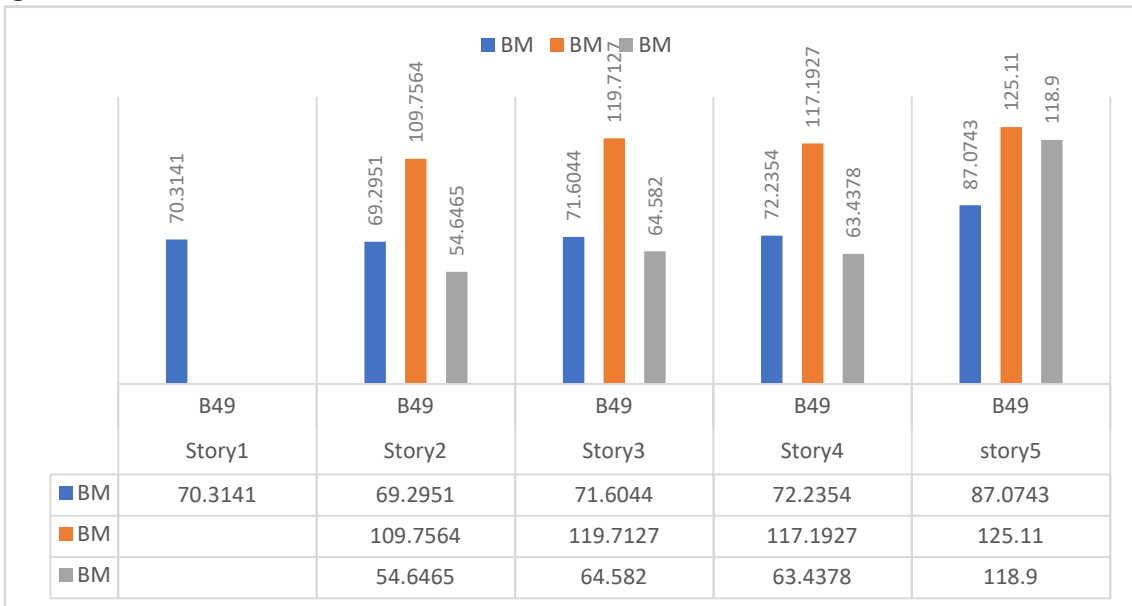
Bending moment for beam no b7



Bending moment for beam no b8

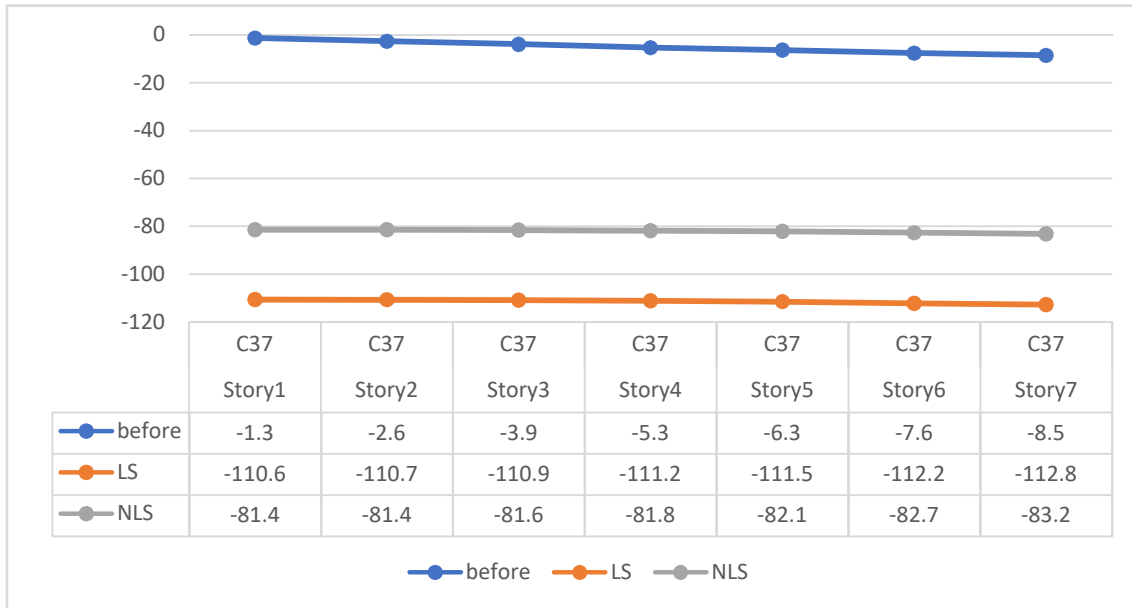


Bending moment for beam no b49



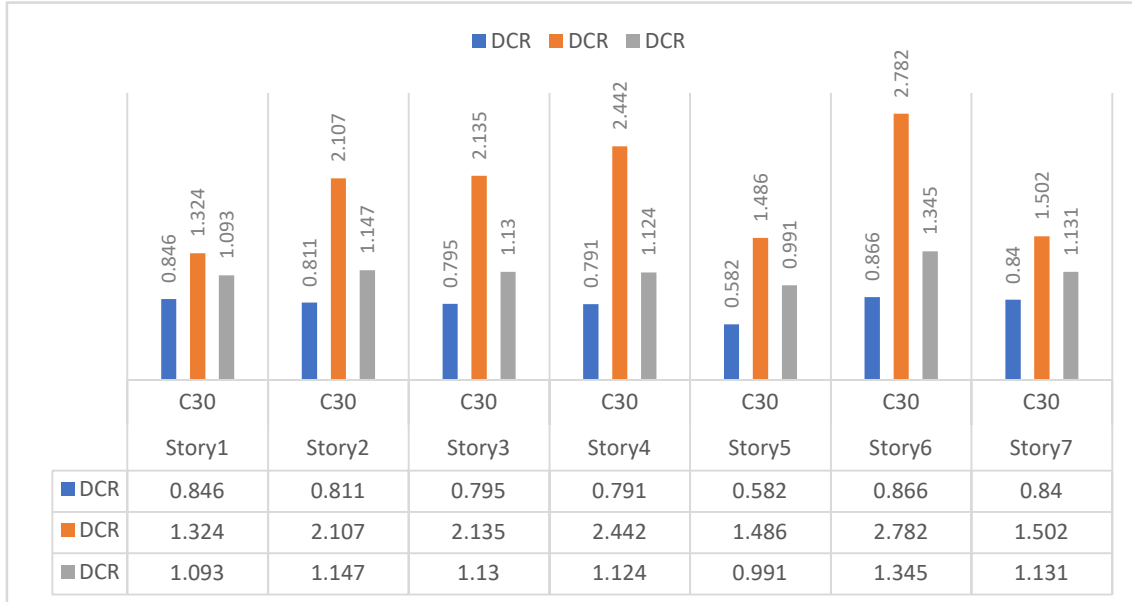
From all above graphs shows that bending moment for before removal of column are in a range between 70 to 90 kn but after removal of column there is an drastic change in linear static analysis as compared to nonlinear static analysis.

Graph 4:displacment,DCR,bending moment for column no. 37 (5x7)
Joint displacement for column no 37

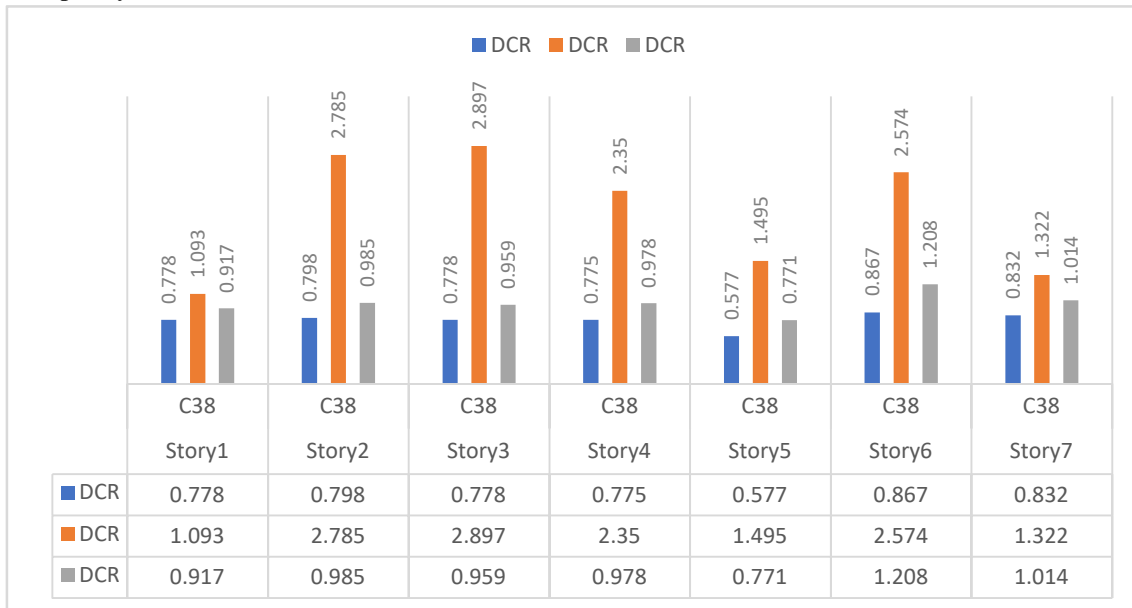


Joint displacement of column c37 before column removal was -1.3mm but due to sudden loss of column c37 and after linear static joint displacement was suddenly increased to 110.6mm and after nonlinear static analysis is -81.4 mm due to less load carrying elements carries extra load.

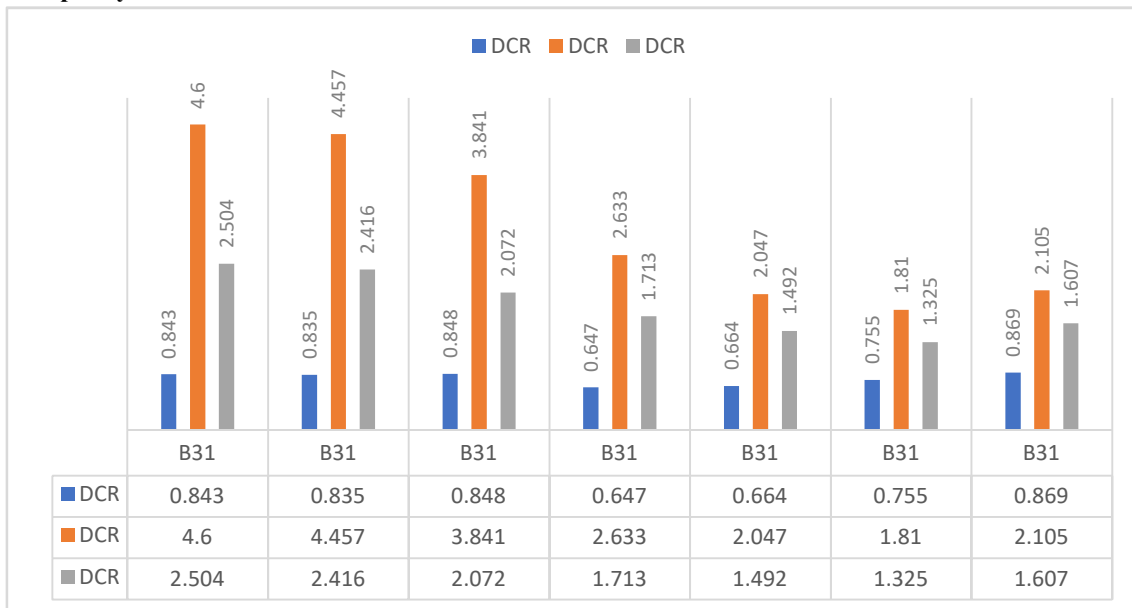
Demand capacity ratio for the column no c30



Demand capacity ratio for the column no c38



Demand capacity ratio for the column no b31



VI. CONCLUSION

- From result it has been observe that as displacement before removal of columns very small after removal these displacement are largely increase in case of linear static analysis as compare to nonlinear static analysis because dynamic increasing factor so large.
- From graph d.c.r. value of adjacent beam are considered and the structure for all combination we maintain DCR of all of structural element is in between 0.5 to 0.9.after removal of column there is an drastic change in DCR of adjacent beams in linear static analysis as compared to nonlinear static analysis.
- It has been conclude that there is an gradual increase in bending moment before removal of column but there is an abruptly change in bending moment in linear static analysis as compared to nonlinear static analysis

- Sudden increase in shear force and bending moment values indicate increase in the strength of beam to avoid the progressive collapse in a structure. Therefore, even though it is a very basic model simulation, it gives in depth fundamental understanding about the progressive collapse
- Nodal displacement for lower height of structure is more as we increase the height of structure the displacement goes on reducing.
- Demand capacity ratio of nearer to removal location is maximum for restructure changes with respect increasing height of structure.
- Bending moment at corner location of lower storey structure is maximum as compare to other two cases.
- Height of structure affect the collapse behavior as height increases progressive collapse decreases which is seen from d.c.r.values, joint displacement, and bending moment.
- It is observed that when an element is removed loads are distributed to its surrounding elements and maximum effect is on neighboring horizontal and vertical elements which defines a progressive collapse.
- Demand capacity ratios for nearby column and beams clearly seen for maximum changes occurs in nearby removed locations; nodal displacement of joint changes abruptly which indicates that beam-column junction becomes critical.
- All the results discussed show the increase in various parameters in the member just in the vicinity of the vertical element removed.
- Further extensions of this research work can includes similar portal frame analysis with and with out different types of bracing for all analysis technique such as linear static ,nonlinear static, linear dynamic, on-linear dynamic analysis for three dimensional frames are also being considered with material non-linearity

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